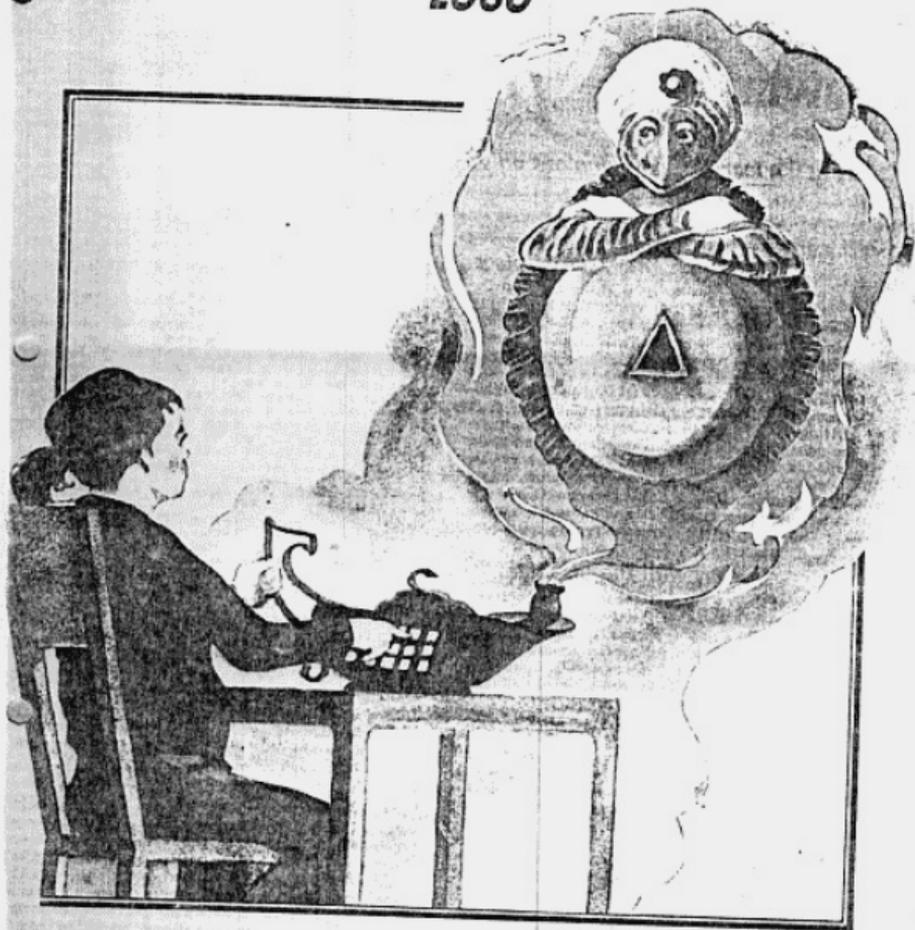


4  
LOGO

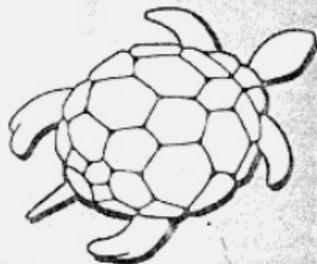


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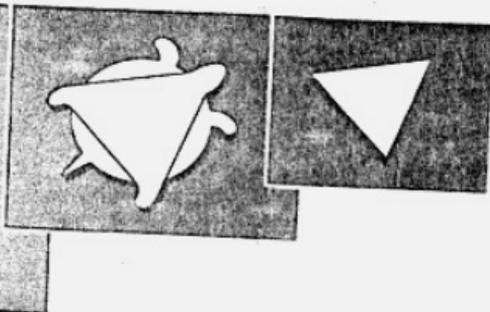
## LOGO

### A learning environment on your Home Computer.

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LAREDO



# The History of LOGO

**L**OGO—a powerful, high-level computer language designed for educational purposes especially as a programming language suitable for young children—is now available on Texas Instruments' TI-99/4A Home Computers. For more than a dozen years, the LOGO Group at the Massachusetts Institute of Technology has been developing the LOGO language and related computer programming activities. Under the leadership of MIT Professor Seymour Papert, LOGO activities have been used with children as young as nursery school age, with MIT undergraduates, and with many students of all ages in between. The philosophy of LOGO's developers has been: "No threshold, no ceiling." A beginner can make the computer do something meaningful and interesting in the very first programming session. Yet at the other extreme, LOGO is suitable for very advanced programming projects.

The philosophy of LOGO has been derived primarily from two sources: The developmental theories of the late Swiss psychologist, Jean Piaget (with whom Seymour Papert worked for several years before coming to MIT), and ideas from a modern scientific field called Artificial Intelligence. From Piaget comes the idea of creating learning environments in which most of what children learn can occur naturally—in the same way children learn to speak their native language, walk or run, and play ball. From Artificial Intelligence comes ideas about ways to use programming languages to aid thinking and problem-solving. Programming a computer in LOGO is seen as the act of teaching the computer a set of new commands, based on what it already knows how to do. Each user is, in effect, creating his or her own computer language, to suit his or her own purposes. Readers interested in learning more about these ideas should read *Mindstorms*, a recent book by Seymour Papert, in which he develops and extends the vision of the relationship between computers and learning that led to his development of LOGO.

LOGO activities are designed to allow use of the computer in a way that is personally meaningful to the user. Activities developed by the MIT LOGO Group have included using a computer to control the behavior of a robot tur-

tle, to draw pictures and explore geometric environments on a TV screen, to create computer animations, invent interactive computer games, compose, arrange, and play music, and produce "poetry." The best known LOGO activity is using a simulated robot turtle on a TV screen to produce geometric designs and cartoon-like drawings. Hundreds of children have learned computer programming and problem-solving skills and developed mathematical expertise while writing programs for the turtle.

The LOGO language includes commands to make the turtle move and draw pictures. A student drawing with the turtle can make it move around on the TV screen by typing familiar commands such as FORWARD and BACK or RIGHT and LEFT. The information which beginners need to control the turtle is already present in their own body knowledge of how to move forward or back and how to turn right and left. Programming becomes an extension of something a learner already knows—rather than something requiring the mastery of an elaborate technical language or a complex coordinate system. The turtle becomes for the learner what Seymour Papert has called "an object to think with." Students using the computer as a programming tool become more aware of both their own body motion and the behavior of the computer.

The version of LOGO developed collaboratively by Texas Instruments and the MIT LOGO Group for the TI-99/4A includes an entirely new graphics environment called a "Sprites World." Sprites are small objects that can move rapidly around the screen, changing shape, color, speed and direction. Large numbers of sprites can appear at the same time to produce exciting animated designs or to be used as elements in programs to create video games. Because of its inherent attraction for so many people and because of the geometric and problem solving ideas embedded in it, the Sprites World promises to be one of the most exciting computer-based learning environments yet invented.

## The World of the Turtle

Let's take a closer look at what actually happens when someone learns to program a computer using the LOGO turtle. The turtle responds to simple commands typed at the

keyboard: FORWARD 100, BACK 50, RIGHT 90, LEFT 45, etc. FORWARD 100 moves the turtle forward "100 turtle steps," drawing a line on the TV screen in the process. LEFT 45 makes the turtle rotate 45 degrees to its own left. People learning LOGO find it natural to "identify" with the turtle, imagining themselves going through its motions as it carries out a particular task. At the same time, controlling the turtle becomes a metaphor for controlling the computer itself: Like the turtle, the computer responds to an ordered series of command, and "TO" procedures that are defined as series of commands.

The ways in which the actions of the turtle can lead to geometric designs, as well as the method used to define procedures, is illustrated in the following simple examples. The turtle can draw a square by repeating the commands FORWARD 100 RIGHT 90 four times. A procedure can be defined by choosing a name (BOX, for example) and typing in a series of commands in order.

```

TO BOX
FORWARD 50
RIGHT 90
FORWARD 50
RIGHT 90
FORWARD 50
RIGHT 90
FORWARD 50
RIGHT 90
END
  
```

To execute BOX enter the following:

```

TELL TURTLE
BOX
  
```

When the new command, BOX, is typed, the turtle immediately draws the shape shown in the figure. (The small triangle shown in the figure represents the turtle by showing its position and heading). A similar procedure, TRI, can be defined as follows:

```

TO TRI
FORWARD 50
RIGHT 120
FORWARD 50
RIGHT 120
FORWARD 50
RIGHT 120
END
  
```

To execute TRI enter the following:

```

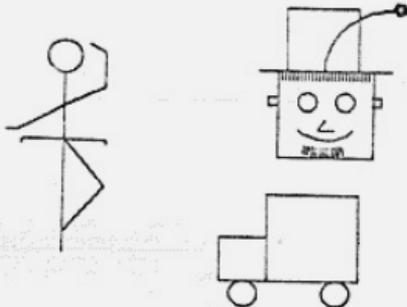
TELL TURTLE
TRI
  
```

A student who has defined procedures such as BOX and TRI is beginning to "teach the computer" his or her own private language. BOX and TRI can now be used in the same way as other LOGO commands. They can be used to create other drawings such as a simple "house" or an abstract geometric "flower."

This approach to geometry and programming provides the basis for a rich universe of activities known as Turtle Geometry, which includes cartoon drawings (simple and complex), geometric designs, mathematical theory building, and computer games. Extensions of Turtle Geometry have proven fruitful when used with advanced high school students or MIT undergraduates. The universe of Turtle Geometry provides a conceptual framework for such aspects of mathematics as the relation between shapes and angles, coordinate systems, positive and negative numbers, the use of variables, symmetry and similarity, and even calculus and differential geometry. The computer programming involved in beginning LOGO activities can include procedures and subprocedures, the naming of procedures and variables, pro-

cedural hierarchy, recursion and iteration, the use of conditional logic, and the development of problem-solving strategies.

Within the universe of Turtle Geometry, there is room for different students working individually to create their own sub-universes or *microworlds*. They can do this with their own limited (but expandable) sets of concepts and related activities and projects. To teach LOGO is really to help learners create, explore, and extend their own microworlds.



I have used turtle geometry as an example of what can be done with LOGO because it is easy for a reader to visualize the commands and to see how they lead to procedures that produce the results in the pictures—just as it is for young children. Children learning LOGO have actually carried out many other types of projects as well: moving turtles, finding their way around race-tracks or mazes, animated cartoons, interactive computer games such as Nim or Tic-Tac-Toe, programs which generate sentences or poetry (or even play Mad-Libs), and programs to translate English into Morse Code, or vice-versa. As LOGO becomes available to owners of TI-99/4A computers, I hope that these pages can be a forum for describing your LOGO projects. Since there will soon be more LOGO users than ever before, we can expect more and different LOGO projects to emerge. One of the best ways to build the culture of LOGO is for users to share project ideas through the pages of books such as this or magazines such as *99'er Home Computer Magazine*.

Although TI LOGO is a recent entry to the LOGO World, a prototype version has already been tested with hundreds of students between the ages of three and nine at the Lamplighter School in Dallas, Texas, and by students in fifteen elementary and junior high schools in New York City. Using the Spites World of animated graphics activities, these students are busily creating a new universe of LOGO activities to delight and educate a new generation of computer users. In an age in which computers are omnipresent in society, and in which universal computer literacy is a pressing national need, computer-based learning environments like LOGO have become essential to the process of growing up literate in the last decades of the twentieth century.

ETC



## The Lamplighter LOGO Project

“A child is not a vessel to be filled, but a lamp to be lighted.” The quote from Alexandrov is on the plaque outside the Lamplighter school. That sign advises any visitor that the school is very unusual.

The curriculum at Lamplighter is individually tailored to meet the needs of each student. Individualization is applied in science, language arts, math, drama, music, art, French, and physical education. The Lamplighter is strongly supported by the parents of its students and by its alumni, with graduates of Lamplighter frequently dropping by to see their former teachers. Such alumni loyalty might not be considered unusual, except that the Lamplighter classes begin with preschool (age 3) and end with the fourth grade-level.

The physical arrangement of the school reinforces its approach to learning. Classrooms have only three walls; the fourth side of each class opens onto an airy, bright shared space. Class rooms are clustered around these shared-spaces by grade-level. Inside each classroom there are tables and chairs for writing work and, on one side, a small tiered well which is used for many other activities (e.g., reading, French, music, or story telling). The staff, the facilities, the students, and the parents all contribute to make Lamplighter a very special private school.

Lamplighter has been a leader in the use of new technology for learning. Calculators, *Speak & Spells*, Systems 80 units, and Little Professors are abundant throughout the school. Students regularly use these learning tools and other learning games found in the shared spaces. Teachers make extensive use of slides, films, and video and audio tapes. When Mr. Erik Jonsson (co-founder of Texas Instruments and Lamplighter Board of Directors Chairman and benefactor) first proposed introducing computers into Lamplighter, his idea was well received. Mr. Jonsson had earlier been in contact with Dr. Seymour Papert

of the Division for Study and Research in Education (DSRE) at MIT, and found the LOGO language and philosophy of learning intriguing. Papert's initial explanation that LOGO allowed students to program computers and not vice-versa, enjoyed a favorable reception from the Lamplighter faculty. Later, as Papert elaborated on the LOGO philosophy, it became clear the LOGO was very much in accord with the philosophy and practice of Lamplighter.

In the fall of 1978, Papert and several others from DSRE made a series of preparatory visits to Lamplighter to arrange for the introduction of LOGO to the school. The plan was to begin LOGO training for first the faculty and then the students by using the Digital LSI-11 LOGO (in use at the Brookline, Massachusetts, project) and later, bring TI LOGO into the school as it developed.

Shortly after the first visit by Papert, Lamplighter rented the first of two LSI-11's that were to be used in the initial two years of the project. Training sessions helped the initial core of Lamplighter faculty (representing nursery school, second grade, third grade, and fourth grade) become familiar with LOGO. This “Computer Group” then began working with third and fourth grade students. Shortly thereafter, a second LSI-11 was rented, and by the end of the spring term every third and fourth grade student had had at least one hour of LOGO instruction on a computer.

The third and fourth graders considered it a treat to work on the computer—partly because these special computer activities allowed them to miss classes, and partly because they genuinely enjoyed working with LOGO. One student's remark reflects the sentiments of many of these pupils. After he had spent an hour working at figuring line lengths, turn angles, and sections of arcs in order to construct a computer picture of a cat, he thanked me for “getting out of math class.”



In the summer of 1979, the Computer Group was expanded, and two workshops were held to refresh the teachers' memories. Subsequently, a 10 day workshop at MIT introduced the teachers to more elaborate LOGO programming and allowed them to participate in discussions on the relationships between learning and LOGO. Then, as the new school year started, the teachers were really surprised to discover how little the fourth graders had forgotten about LOGO. These students generally recalled all of the commands they had learned three months earlier—even though they had had no contact with LOGO in the interim!

Midway through the fall semester of 1979, several early prototypes of TI LOGO were tested at Lamplighter and revised by the MIT LOGO laboratory personnel in consultation with Lamplighter and Texas Instruments. In January 1980, the pace of computing at Lamplighter accelerated as an updated version of TI LOGO was implemented on the TI prototypes. By the end of January, a dozen prototypes were in use at Lamplighter, and a very few students continued to use the LSI-11 LOGO. Most pupils, in fact, switched to the TI prototypes even though that meant re-learning much of LOGO.

In the middle of the spring semester, a few more prototypes arrived and all the machines were upgraded to a later version of TI-based LOGO. Before the school year ended, all of the third and fourth graders had had at least one hour on the new machines. One of the rented LSI-11's was then returned (though few noticed its departure). At that time, several fourth graders were writing elaborate programs which made use of recursion to create "movies" or "rain-bows" (changing colors), or elaborate scenes. Some students were so taken with LOGO that their parents happily bought them their own computers (at that time, TI LOGO was not yet commercially available); other students became

enthralled with their ability to produce perfectly printed letters and numerals on a keyboard and later received typewriters as presents from their parents.

By September 1980, a total of 50 TI LOGO prototypes were in operation at Lamplighter. The version of LOGO on these units was very close to that which TI is now marketing. Then, late in the fall, the second LSI-11 was returned, but its loss went completely unnoticed because all of the faculty and student interest was already focused upon the TI LOGO prototypes. Since September, the Computer Group has continued to work individually with third grade students. In addition, the rest of the faculty is being trained in LOGO, and it has been introduced into all of the classes as part of the regular school curriculum.

The teams at each grade level decided the best way to introduce LOGO into their classes and worked out various procedures for that introduction. For example, one teacher developed special simplified LOGO programs for the preschool children which required less typing in order to produce interesting effects. And personalifications of LOGO constructs made LOGO easier for first and second graders to understand. Currently, students can be seen at every shared-space LOGO machine during lunch-hour, before school, after school, and whenever other school activities are completed. For the rest of the semester, LOGO will be used in class by the teachers as they feel it is relevant for their lessons and will continue to be available (as are the other learning aids) to students during free periods.

The Lamplighter LOGO project was not intended to be a formal experiment. Since there are no control groups, strong causal claims for LOGO's effects are inappropriate. Several cognitive and psychological assessments, however, were made at the beginning of the project and will be made again at the conclusion of the present school year. And, there already have been some indications of student attitude and behavior change. This is best exemplified by the way in which the pupils express their keen interest in acquiring new LOGO knowledge.

It's always interesting to observe what motivates children to learn. Because LOGO is so extensive, Lamplighter teachers find it impossible to show students all the commands in the initial sessions. As a result, students have taken the discovery of more LOGO commands as a sort of treasure hunt and this new, "unauthorized," LOGO information is disseminated through an "underground network" among the students. During a training session in which teachers were learning to use MAKESHAPE (the LOGO command with which users make their own shapes on a 16 x 16 grid), some students were secretly watching them. Shortly afterward, a hand-copied "underground" LOGO manual with clear and concise directions for the use of MAKESHAPE was found on the floor of a classroom; at the same time, a number of students began using MAKESHAPE.

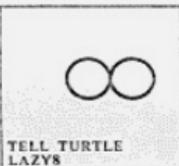
Students have discovered other information accidentally. One student typed MC instead of MS for MAKESHAPE; this put him in MAKECHARACTER mode. In this mode, LOGO users can modify old characters, or make new characters. The student proudly shouted out his discovery to his classmates, who quickly confirmed his results and spread the news. New information has diffused from grade to grade or class to class or from parent to child in a similar manner.

Sharing among peers is the overwhelming response of Lampfighter students to new LOGO information. Pupils eagerly and proudly explain their accomplishments in LOGO. At first, however, there were a few exceptions. A couple of students were secretive about some LOGO information and effects. One student made the screen's background color black so that no one could read what he typed; another tried to *scfi* LOGO programs to his classmates! After they discovered that other students could find different ways to achieve the same effects and were willing to share, they started sharing as well.

In at least one case, LOGO seems to be responsible for a major behavioral change. Late last year, a fourth grader who had not been performing well academically, and who had been somewhat disruptive in class, started programming in LOGO. As he played on the computer, his typing became very fast (QWERTY keyboards are quite properly regarded by the Lampfighter children as a stupid arrangement with which they reluctantly work), and his program became sophisticated. He was heard to remark, "I can't believe how fast my fingers are typing." He also could not believe how much fun school had become. Not only did he do well with LOGO, but he also became an attentive, productive student.

Figure 1.

```
TO LAZY8
FORWARD 4
RIGHT 90
TEST HEADING = 0
IF LAZY8
FORWARD 4
LEFT 90
END
```



**Comment:**

TEST checks the heading of the Turtle. If it's not 0 (North), the Turtle continues to draw the LAZY8.

After finishing the right-hand circle, the heading becomes 0 and the left-hand circle is drawn.

To really understand why the left-hand circle over gets completed, you have to know something about microprocessors and stack operations. In keeping with the scope of this section, however, a simple anthropomorphic explanation will have to suffice at this time. Other sections will take an in-depth look at the technical aspect of the language.

*Think of the job of drawing the LAZY8 as being given to a group of little workmen inside the computer. The first workman carries out the first four lines then decides he needs a rest before continuing. Notice that in his initial contract TO LAZY8 he has agreed to eventually carry out the FORWARD 4 and LEFT 90 specifications. The work must go on while he rests, so he subcontracts out the next stage to another little man. This workman also carries out the first four lines, then he too decides to rest. So before he gets to the FORWARD 4 LEFT 90 tasks, he decides to subcontract out the balance of the work on the right-hand circle. This process goes on with enough little workmen (16 in this case) until HEADING = 0. At that time, the last little man carries out his FORWARD 4 and LEFT 90 tasks, and gives the job responsibility back to the next-to-last workman who also carries out his remaining FORWARD 4 and LEFT 90 tasks. This reverse process of finishing the last two tasks and relinquishing responsibility goes on until the original contractor finishes his original job with a single FORWARD 4 and LEFT 90, thus completing the left-hand circle in the LAZY8—Ed.*

At present, most of the third and fourth graders—and even some of the first and second graders—are writing LOGO programs. And this includes some fairly sophisticated programs which use recursion and the concept of state transparency. A few children even acquired the skill of using *subprocedures*—i.e., breaking a complex program down into its several component parts. This is one of the most important features of procedural languages such as LOGO. Most students had discovered recursive programming, or "cursives" as a few called it. In recursive programs, one of the program lines calls for a new stack to execute the program again. You do this by including the name of the program within the program itself. All the recursive programs written by the students, however, had the recursive step in the last line. [When the recursive step occurs in the last line before END, the procedure is said to have "tail-end recursion." For an example of somewhat more sophisticated usage, see the LAZY8 procedure in Figure 1—Ed.]

A number of programs produced exciting video scenes. In EXPLODE, 32 differently colored balls splay out from the center of the screen before repeating the entire procedure. One third grader saw how he could place a program which printed a message inside EXPLODE, and thus combined recursion and subprocedures. RAINBOW had one or more sprites continuously change colors for an attractive visual effect. There were also programs which had the TV monitor take on a series of sixteen colors, and programs which changed the background of the screen to black and created unusual perceptual illusions by shooting light-colored shapes across the screen. Some even had jets, rockets, or airplanes spouting fires from their engines.

Other children wrote programs which put shapes together to create scenes, such as a home with a car driving down the street in front of the home. Most students had written utilitarian programs like VANISH (Figure 2) which caused the sprites to move off screen. Take on the clear color, carry an empty shape, and which caused all the printing to be cleared from the screen.

Figure 2.

```
TO VANISH
TELL TURTLE
CARRY 0
SETCOLOR 0
SETSPED 0
SETHEADING 0
END
```

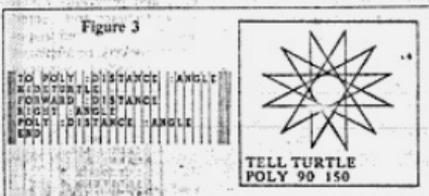
After spring break, several things happened which caused a quantum leap in the computer work of the students. First, the children were shown how to save their programs and shapes on cassette tape. Until then, the students had to write in their computer notebooks anything they wanted to save. That meant that any elaborate shape had to be reproduced on a grid in an arduous manner, and long programs or complex programs required a very long time typing. (Remember these children are elementary pupils with little typing experience before computers!).

Students had not used much of their work as foundations for future work simply because loading the old material took so much of their time. Now, with the recorders, they could use and improve each session's programs just by taping and playing back a cassette. Also, they could design and SAVE complex shapes instead of seeing them lost when the computers were shut off.

The children were also shown the TELL TURTLE mode. This opened up all of the turtle geometry features of LOGO.

(Turtle geometry is such a powerful idea that some Pascal systems have adopted it.) This newly acquired mode, coupled with the previously learned SPRITE MODE, allowed the students to produce many interesting programs and visual effects. As a result of these new developments, many of the students soon exhibited a feeling of mastery over the computers.

In the final eight weeks of school there was an exponential explosion in the complexity of the students' programs and in their ease with the machines. They quickly learned to use variables as inputs, and consequently "discovered" the famous turtle geometry POLYgon program which can generate any regular polygon. (See Figure 3.) Then one student found that changing the angle of the turn on each recursion could produce beautiful patterns—including a striking nested curl in a star pattern. Many students now began putting programs together in subordinate and superordinate structures. Programs contained the unique LOGO controls of TEST, IFT, and IFF, as well as the conditionals IF-THEN-ELSE, plus BOTH and EITHER for conjunctive and disjunctive branching. One of the third graders wrote a CAI (Computer-Assisted Instruction) program to quiz his first grade friends on addition facts using these control commands! He then added visual displays of the addends, and encouraging remarks when a student made a mistake, or a colorful scene as a reward for the correct answer.



Using combinations of several user-drawn shapes, students began constructing very elaborate composite pictures. One third grade student also discovered how to change the characters associated with each console key [by redesigning the characters on a grid "tile" with the MAKECHAR primitive—Ed.], and decided to tease the teacher. She replaced the 3 with a 2, and then called a teacher for a demonstration. While instructing the computer to print  $3 + 3$  (which now looked like a request for the sum of  $2 + 2$ ), she remarked to the teacher: "Look how dumb this computer is... it doesn't know  $2 + 2$ ."

The activity among the third grade students was exciting to witness. One began programming dramas in which text was printed at the bottom of the screen while the story was enacted in SPRITE and TELL TURTLE modes at the top of the screen. One other third grader was so intrigued by the space shuttle's landing that on the same afternoon of the landing, he began working on a shuttle program. First, he used MAKESHAPE to construct a faithful replica of the shuttle, complete with USA monogram, black-and-white coloring, and auxiliary rocket engines. Then he worked for part of the afternoon and a little of the next morning to write and debug his programs. His final superprocedure

launched the shuttle with flames shooting from the engines, jettisoned the auxiliary tanks, orbited the shuttle around planets in outer space, returned the shuttle to a dry lake-bed runway, taxied it to the end of the runway, and stopped it for a perfect landing. His programs are shown here in Figure 4

Figure 4

Note:  
BG = BACKGROUND  
FD = FORWARD  
SC = SETCOLOR  
SH = SETHEADING  
SS = SETSPEED

```

TO TAKE
  TELL 1 CARRY 20 SC 15 HOME
  SN 90 FD 15
  TELL 2 CARRY 21 SC 15 HOME
  TELL 3 CARRY 22 SC 15 HOME
  SH 270 FD 18
  TELL 4 CARRY 23 SC 8 HOME
  SN 270 FD 32
  END

TO SHUTTLE
  TAKE
  PLANE
  FLAME
  END

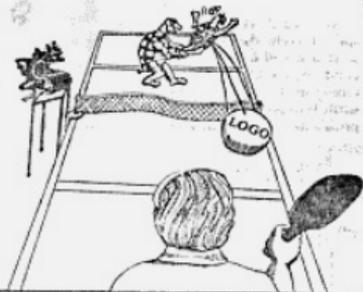
TO PLANE
  TELL 5 CARRY 24 SC 15 HOME
  SN 0 FD 10 SN 90 FD 16
  TELL 6 CARRY 25 SC 15 HOME
  SN 0 FD 16
  TELL 7 CARRY 26 SC 15 HOME
  SN 0 FD 16 SN 270 FD 16
  TELL 8 CARRY 27 SC 15 HOME
  SN 0 FD 16 SN 270 FD 16
  TELL 9 CARRY 28 SC 15 HOME
  SN 180 FD 47 SN 18 FD 12
  TELL 10 CARRY 4 SC 8 HOME
  SN 0 FD 25 SN 270 FD 23
  TELL 11 CARRY 4 SC 8 HOME
  SN 90 SS 20
  TELL 30 SC 1
  END
  
```

(Note: listings of TI LOGO procedures are just that—listings of procedures. There's no way to print out a transcription of the data needed to MAKESHAPE and MAKECHAR as can be done with the HEX Codes in TI BASIC and Extended BASIC. The only way to show the graphics that a program contains is to show it as drawn on a series of "tiles" on the grids that appear on screen when the shapes and characters are first displayed. This is similar to CHARGE3 routine in Programming Aids 1. The listing of the Space Shuttle program was included (without the tiles) in this article to demonstrate the simplicity of the language structure.—Ed.)

The gains made by the Lamplighter children with LOGO have indeed been impressive. They confirm Papert's dictum [*Mindstorms*, Seymour Papert, Basic Books 1980] that children should program computers and not vice-versa. It's obvious that LOGO has indeed furthered Lamplighter's goal of igniting the imaginations and intellects of its children. But more importantly, LOGO has the potential to fire up imaginations everywhere.

# Who is LOGO For?

Its not just for  
Turtles anymore . . .



Recently the question of LOGO's relevance for children and its relevance for adults has been stated as an implicit either/or issue. That the issue ever arose means that people (including me) who write about LOGO have not done their jobs as fully as they should. Perhaps the notion that LOGO was just for children developed because of the total attention children invest in LOGO. The position that LOGO is too complex for children may have arisen because published programs seem magic unless one actively explores them (including seeing what happens when the programs are changed). Presenting a program as a *fait accompli* to be copied, run, stored, and used like any other software is contrary to the philosophy of education behind LOGO.

LOGO is for humans. When Papert asked me if I felt comfortable with my LOGO, I said that LOGO is like a hologram—when you grasp just the smallest part of it, you have a small, but complete picture; and later as your understanding grows, you still have a complete picture, albeit larger. From that perspective, people can always learn more from LOGO and do more with LOGO even though they are able to use LOGO after the briefest of introductions. This feature of LOGO is what Papert alludes to in his slogan, "Low threshold, no ceiling."

The LOGO slogan invites empirical verification. In my self-observations and studies of other adults, I have noticed that there are common, identifiable LOGO-developmental stages. Among these are the discovery of heuristics (i.e., powerful ideas), improved understanding of numbers, appreciation of angles and heading, and awareness of states and state independence. Probably the greatest gain people share in working with LOGO is the realization that one can find out on the computer, rather than ignoring the question or looking the answer up somewhere. This is so obvious that it might appear trivial; it is not. All learning theorists agree that active learning is preferable to passive learning. This presents a dilemma for those writing about LOGO: How do you capture the open activity of a LOGO learning enterprise in a closed article?

The purpose of this article, however, is to reflect the development of a LOGO game, and in that development show how an apparently complex program is child's play, even for adults. At the same time, I hope that the development will point to variations and will entice you into active exploration. The program was initiated by a student in a course I taught.

The program was supposed to be a "Pong" type game. As you follow its growth, find the point, if there is one, where the program stops being a children's program.

The game begins not as a program, but simply a collection of conditions.

```
TELL [0] BALL  
GARRY [BALL  
SETCOLOR [PADD  
SETREADING [R  
SETFIELD [S  
[HOP]
```

These commands set a ball speeding left-to-right across the middle of the screen.

The idea grows into a program as the ball is set to "bouncing" off left and right boundaries. This is accomplished any of several ways:

```
TO BOUNCED  
TELL [0]  
TEST [COR > 85  
LEFT RIGHT 180  
TEST [COR < -85  
LEFT RIGHT 180  
BOUNCED  
END
```

But BOUNCED sometimes doesn't work—occasionally the sprite is "caught" at one end or the other. What happens is that the sprite slips past one of the boundaries (e.g., the computer is at line 2 of the program as the sprite moves left through X coordinate equal to -85; by the time the computer reaches line 4, the sprite is well left of X coordinate -85. Then the computer turns the sprite right 180 (a right 180 functions equivalent to a left 180). Before the sprite can move beyond the -85 X coordinate, the computer checks line 4 again, turns the sprite 180 and sends it still further to the left. Of course, when the computer reaches line 4 a third time, the sprite is still left of -85; the poor sprite is stuck beyond the left-hand boundary! This bug could be eliminated with a second type of BOUNCE program:

```
TO BOUNCED  
TELL [0]  
TEST [COR > 85  
LEFT [REAR 180  
TEST [COR < -85  
LEFT [REAR 180  
BOUNCED  
END
```

that the CHECK program is invoked only if the ball is beyond XCOR 85. Therefore, part of the scoring and noises can be controlled after line 3 of BOUNCE2 by rewriting the CHECK program:

```

TO CHECK
TELL 0
TELL CALDALTOUNG
IFP CALL 1P15 1 0 3 1
IFP INCREASE 1 1 PLAYER'S SCORE
IFP NOISE 1 NOISE FOR THE
  PLAYED'S POINT
IFP DECREASE 1 1 300
IFP ONLY 1P15 1 1 1000 2150
  INCREASE COMPUTER'S SCORE
IFP BEEP WAIT 10 NOISEP 1 A
  SOUND BEEP FOR COMPUTER'S
  POINTS
TYPE (YOUR SCORE IS 1 PC 3)
TYPE (PLS PC 3)
TYPE (THE COMPUTER'S SCORE IS
  PC 3)
PRINT 0P15 1 1000 2150
WAIT 50 PLS 1 1000 2150
EXTRA SCORING OR SACK BEEPS
END
  
```

```

TO NOISE
REPEAT 5 (BEEP WAIT 1 NOISEP 1
  A)
END
  
```

It is necessary to set up an initial value for both the computer's score and the player's score as was done with :Y. Since this is done just once, it belongs in SETUP. [The initial score is 0 to 0—as in the proverbial “soothsayer’s” prediction or score before it begins. . . .] So SETUP is revised:

```

TO SETUP
TELL 0
CARRY 0 BALL
SETCOLOR 0:0:0
MOVE1
SETREADING 99
SETPEEK 85
TELL 0 1 1
CARRY 100
SETCOLOR 0:0:0
SETREADING 0
SET 100 0
TELL 2
SET 10
CALL 10 1 1
CALL 0 0 100
CALL 0 0 100
END
  
```

This game, like most LOGO projects, is open-ended. It could be altered so that a winner is named at a score of 21, revised for two players, changed to use joysticks or changed so that the ball has topspin. With each addition, it is necessary to make sure that the initial conditions are established only once, that procedures to be repeated are placed inside a recursive program, and that there are no Recursion Interface Bugs.

```

TO BOUNCED
TELL 0
TEST SCORE > 85
IFP CHECK 1 1 85
TEST SCORE < 0
IFP BOUNCEDING 0 0
TEST SCORE < 99
IFP BOUNCEDING 1 85
TEST SCORE < 85
IFP BOUNCEDING 0 5
END
  
```



# LOGO's

# POWERFUL

# SURPRISES!

## PART 1: Language Structure and Syntax

**L**OGO was developed by Seymour Papert and his associates at the MIT Artificial Intelligence Laboratory in order to study the way people might learn in a computer-rich environment. It was designed to be a language so simple to use that a person could manipulate objects or concepts by just thinking about what he or she wanted to accomplish, and not have to worry about programming. Such a language might stimulate a person to explore, to learn, and to grow.

The idea was to provide certain *primitive* commands and operations that could be combined to form more *complex* commands and operations. These more complex ones could then be used exactly like the primitive ones. Thus it would be possible to construct a single command to accomplish anything that could be accomplished using the primitive concepts. Additionally, *recursion*—whereby a command could call and activate itself—was allowed.

LOGO is a relative of LISP, the list processing language used in artificial intelligence. LOGO and LISP share the capability of manipulating numbers, words (character strings without a space), and lists. A *list* is a recursively defined object: It is an ordered set of objects, each of which may be a number, a word, or a previously defined list. In LOGO, a *procedure* is represented by a list; there are commands to access a list that represents any procedure, and to define new procedures from lists which might be the result of some manipulation. Furthermore, a procedure may have inputs and may have an output, and is activated by specifying its name (a word) followed by its inputs (which may be numbers, words, or lists). Defined procedures as well as primitive commands and operations all have exactly the same syntax. This is why LOGO is so simple to use. Its power comes from its list processing capabilities.

I hope that the description given so far has made it apparent that LOGO is *not* just for children. Although LOGO

can be used in elementary ways, it is much more than FORWARD 20 RIGHT 90. LOGO is a language for all people who want to learn and expand their capacities.

### The LOGO Turtle

The first experiments with LOGO were with junior high school students who could appreciate manipulation of words. Then a Turtle was created whose movements could be understood by very young people.

The Turtle was originally a robot that could be commanded to move about the floor. It had a pen which could be either up or down. In an experiment at the University of Pittsburgh Learning Center several years ago, one young person used LOGO to command the floor turtle to draw an alphabet of large letters. He also taught it to act like an airplane, and "fly" between cities on a large map. The plane had the possibility of going out of control, with the turtle going into a spiral and spinning on the floor. The turtle is now usually a small triangle on a terminal screen, but it can still do such things, albeit on a smaller scale.

At the youngest levels, LOGO is being used to teach a feeling for distances and angles. At levels through college it is being used to advance a new subject in mathematics called "Turtle Geometry." Some interesting theoretical results have come about. (A wealth of examples and exercises is contained in *Turtle Geometry* by Abelson and diSessa, where procedures are expressed in a language almost exactly the same as LOGO.) Recursive designs such as snowflake curves, space filling curves and trees are applications of LOGO's power.

### Tl LOGO

Tl LOGO is marketed as a language for children, and it was a pleasant surprise to discover that Tl LOGO has all of the list processing capabilities built into it. All the recursive designs presented in *Turtle Geometry* can be drawn. (The Tl Turtle is, however, limited to 192 different

8 x 8 pixel character positions. Thus, if a figure is very dense, it can't be very large.)

The documentation that comes with TI LOGO doesn't make it easy to discover LOGO's power. Many of the commands needed for manipulating all but the simplest lists are not documented.

At this point, it may be helpful to briefly describe just what is available to a person who sits down to use TI LOGO. The TI Turtle is an object that lives on a coordinate screen with horizontal coordinates from -119 to +120 and vertical coordinates from -46 to +97. The bottom six lines of the screen are used for text. The turtle can be assigned a position, and "knows" where it is. It can be assigned a heading (from 0 to 360 as the points of a compass) and knows its heading. Its heading can be changed by a given angle, and it can be moved a given amount either in the direction of or opposite to the direction of its heading. It can make a dot at any position. The pen can be down, up, or in "reverse" modes, and it can draw in any of 15 colors.

Unique to the TI version of LOGO are *sprites*—objects familiar to those with TI Extended BASIC. There are 32 sprites (numbered 0 to 31) with each assigned to a 16 x 16 pixel shape. Users may design and store 26 of these and can direct any collection of sprites to assume simultaneously an attribute such as shape, color, position, heading, speed, or velocity. The commands which control the turtle act similarly on the sprites. Motion is controlled by assigning a speed (in the current direction) or a velocity (horizontal and vertical components). Not only can attributes be assigned, but they can also be obtained as the output of operations because a sprite always knows its own number, shape number, color number, position (on the full screen), heading, speed, and velocity.

Papert has described *Velocity Turtles* (which can have velocities) and *Acceleration Turtles* (whose velocities can be incremented). Sprites can be both. Using sprites we can even simulate Papert's "Dynamturtle"—an acceleration turtle which does not change direction when it is rotated, but changes velocity only by accelerating in the direction it is facing, thus obeying Newton's laws of motion. A *dynaturtle* therefore behaves like the ship in the popular *Asteroids* arcade game. The example procedures that follow this article will demonstrate a *dynaturtle* which can have the force of its "thruster" changed, and which can simulate an environment with friction.

TI LOGO also has 256 tiles (numbered 0 to 255) that can be given arbitrary 8 x 8 pixel designs. We can assign tiles foreground and background colors and position them anywhere on the 24 x 32 character screen or on the current print line. Console characters are tiles, the number of each tile being the ASCII code of the character. (Note: The Turtle records its trace using tiles, so simultaneous use of the Turtle and nonprinting characters is limited.)

#### Numbers, Words, and Lists

A *number* in TI LOGO is an integer from -32,768 to 32,767. Numbers can be added, subtracted, multiplied and divided (integer quotient), calculation being modulo 32,768. The restriction to integer arithmetic is a definite limitation, but the limitation is not serious for most applications.

A *word* is a character string without a space. A feature of LOGO, distinguishing it from other programming

languages such as BASIC or Pascal is the capability of using a word *simultaneously* as (1) the name of a command or procedure, (2) a variable, and (3) data. For example, if the word X is to be used as the name of an action, X itself is used. When an object has been assigned to X, the object is denoted :X. The word X as data is denoted \*X. Suppose that X has not been defined as an action and has not been assigned a value. LOGO will respond to X with TELL ME HOW TO X, to :X with :X HAS NO VALUE, and to \*X with TELL ME WHAT TO DO WITH X.

A word can be assigned any kind of data—i.e., a number, word, or list as a value. This also distinguishes LOGO from BASIC or Pascal where the data type of a variable must be specified in advance. As a bizarre example, note that MAKE "MAKE "MAKE and MAKE "MAKE [MAKE] assign to MAKE first the word MAKE and then the list whose single member is the word MAKE.

A *list* is the most powerful data object in TI LOGO and is denoted by a left bracket followed by its members, then a right bracket. Examples of lists are [], the null list; [HOW NOW BROWN COW], a list of words; and [REPEAT 4 [FORWARD 20 RIGHT 90]], a list whose members are a word, a number, and another list.

#### Data Manipulation in LOGO

Commands which are powerful in manipulating data include the following: FIRST(F), LAST, BUTFIRST(BF), BUTLAST(BL), SENTENCE(SE), FPUT, LPUT, NUMBER?, WORD?, THING?, THING, WORD, MAKE, RUN, TEXT, DEFINE. The last three are used to execute a list of commands, to access the list which defines a procedure and to define a procedure represented by a given list. These are powerful commands, but to be able to make use of them it is necessary to be able to construct lists whose members themselves are lists. The following key (undocumented) commands, FPUT and LPUT, are helpful here:

**FPUT object list**—outputs a list whose first member is object, and whose following members are the members of list.

**LPUT object list**—outputs a list whose last member is object and whose members all but the last are the members of list.

If *object* is a word or a number, the results of these commands are the same as SENTENCE *object list* and SENTENCE *list object*, respectively. But if *object* is a list, FPUT *object list* adds *object* to the beginning of list while SENTENCE *object list* adds the members of *object* to the beginning of list. This is a crucial difference, making possible the construction of arbitrarily complicated lists. The other commands in the above list which are undocumented are as follows:

**NUMBER? object**—returns TRUE if object is a number, and FALSE otherwise.

**WORD? object**—returns TRUE if object is a word, and FALSE otherwise.

**THING? "name**—returns TRUE if name has been assigned a value, and FALSE otherwise.

THING *name*—returns the object which has been assigned to name, if name has a value.

WORD *word1 word2*—returns the word formed by concatenating word1 and word2. (Compare with SENTENCE, below.)

SENTENCE *wordorlist1 wordorlist2*—(a documented command), returns a list determined by the inputs. If an input is a word, that word is put in the list. If an input is a list, its members are included in the list.

Some of the undocumented commands were found by accident; others by studying the documentation for MIT LOGO. Still others were known to Jim Muller, president of the Young Peoples' LOGO Association (YPLA). We encourage readers to share other discoveries with us.

#### A Calculating Example

As a simple example, consider the problem of teaching LOGO to act like a calculator. If one enters  $2 + 3$ , the response is TELL ME WHAT TO DO WITH  $2 + 3$ . Here, desired output is 5, which is the result of executing PRINT  $2 + 3$ . The problem is solved by using SENTENCE to form the list [PRINT 2 + 3] and then using RUN to execute the list. A solution is the following:

```
TO CALCULATE
  MAKE 'R READLINE
  TEST 'R '0
  IF (=) RUN SENTENCE 'PRINT 'Y CAL
  CALCULATE
END
```

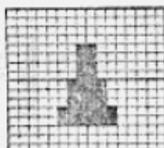
After you enter CALCULATE, the computer accepts arithmetic expressions and prints out the resulting value until just ENTER is pressed. The recursion then "unwinds," and the procedure stops.

The power of a list processing language such as TI LOGO becomes apparent the more you use it. Yet for learning, all of these advanced capabilities *don't* have to be utilized. This is what makes the language so versatile—its built-in power that is accessible on demand. And it is this versatility that allows teachers to tailor LOGO for special applications, and reassures all students that with LOGO there is always more to learn.

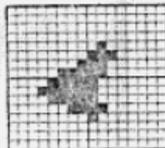


## PART 2: Constructing a DYNATURTLE

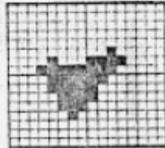
The instructions for using the dynaturtle are obtained by typing HELP. The dynaturtle itself is activated by typing DYNATURTLE. The procedure starts out drawing a circle and displaying a white dynaturtle. Touching the E key



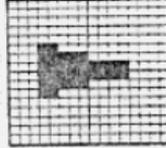
SHAPE 10



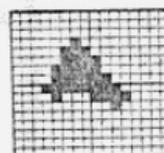
SHAPE 11



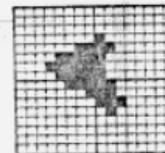
SHAPE 12



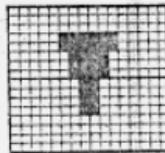
SHAPE 13



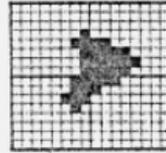
SHAPE 14



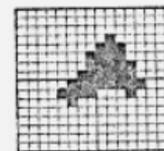
SHAPE 15



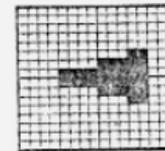
SHAPE 16



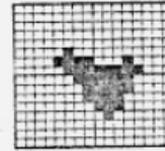
SHAPE 17



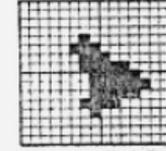
SHAPE 18



SHAPE 19



SHAPE 20



SHAPE 21



# EXT-E-N-D-I-N-G LOGO

## Applications for Very Young Children



Seymour Papert designed LOGO to have a low threshold so that even young children could benefit from it. Unfortunately, the present technical requirement that LOGO input and output be *text-bound* limits LOGO to children who can read and type.

It is apparent that learning in a LOGO environment offers greater potential for pre-verbal children than for verbal humans. This is simply because there is so much more for them to learn. But it is equally apparent that the reading/typing prerequisite is an artificial barrier to that same environment. The ultimate solution—a computer which can comprehend and generate speech—is not yet available. (Programs such as *TX* text-to-speech, however, can do a reasonable job of talking.) Still, there are ways LOGO can be adapted to children who are only able to recognize alphabetic characters or typewriter keyboard symbols.

Even before LOGO was implemented on the DEC LSI/11 or the TI-99/4, people in the MIT LOGO lab worked on simplified LOGO systems. One approach yielded a special LOGO input device which translated symbol cards<sup>1</sup> inserted into slots through a light scanner into ASCII code. Although prototypes of the "slot machine" card reader worked well enough, the idea was never developed commercially. A second approach was followed by Bob Lawler, a graduate student at the time, who wanted his two children to be able to use LOGO. He wrote a number of excellent LOGO programs which allowed very young children to draw with the turtle, to play shoot-out games with the turtle, or to design elaborate turtle pictures. Lawler's programs were written for a large, mainframe computer version of LOGO, but his ideas are compatible with TI LOGO. In fact because of the excellent color graphics of TI LOGO, his ideas may involve children more effectively when set up on the TI-99/4A. The essence of his programs was to simplify access to turtle geometry by simplifying and combining commands. One simplification allows pupils to move the turtle forward or backward a fixed amount, or to turn the turtle left or right a fixed amount by pressing any of the four "arrow" keys:

```

TO DRAW
TELL TURTLE
SIMPLIFY
END
  
```

<sup>1</sup> The cards carry labels like **RIGHT 90**, **FORWARD 10**, as well as symbols for recursion and sub-procedure calls.

```

TO SIMPLIFY
CALL BC ANSWER
IF ANSWER = "D RIGHT 90
IF ANSWER = "F FORWARD 10
IF ANSWER = "X BACK 10
IF ANSWER = "S LEFT 90
SIMPLIFY
END
  
```

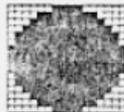
With slightly more sophisticated children, or as children work with DRAW, we can add other commands by merely inserting them into SIMPLIFY. For example:

```

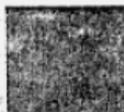
IF ANSWER = "C CLEARSCREEN
IF ANSWER = "Q STOP
IF ANSWER = "P PENNASE
IF ANSWER = "I PENDOWN SETCOLOR 1
IF ANSWER = "4 PENDOWN SETCOLOR 4
IF ANSWER = "U PENUP
  
```

Then, as students master the fuller set of DRAW commands and learn the idiosyncracies of QWERTY typewriter code, they can be introduced to TELL TURTLE without using DRAW any further.

Coleta Lewis, a teacher at the Lamplighter school in Dallas, adapted sprites for use by nursery school children. (The Lamplighter school pioneered the use of TI LOGO with children; see "The Lamplighter LOGO Project.") Two "games" her children played allowed them either to move a garage around the screen, move a car around the screen, and vary the colors of each separately, or to construct a face and then color in the parts of the face. Programming sprites for very young children is not much more difficult than DRAW. As one example of a sprite game for youngsters, consider a game of blocks. It is fairly easy to create a universe of blocks with simplified sprite commands. First, it is necessary to make up some "blocks" using MAKESHAPE. A circle (shape 4) and a square (shape 5) already exist. A good set of blocks ought to have a triangle.



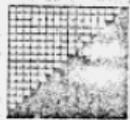
SHAPE 4



SHAPE 5

It would, however, be better to build triangles with four different orientations because the shapes of sprites cannot be rotated.

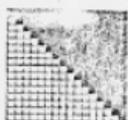
These could be assigned shape numbers 6, 7, 8, and 9. A good block set should also have a rectangle. To show the two orientations, shape numbers 10 and 11 could be designed as shown.



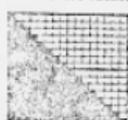
SHAPE 6



SHAPE 7



SHAPE 8



SHAPE 9



SHAPE 10



SHAPE 11

Other shapes could be easily added. Children should be able to color the blocks, move the blocks around, change the shape of any of the blocks, and bring more blocks onto the screen. In addition, when a child begins working with one of the blocks, he or she should be able to identify which one it is. (One way of identification can be aided is to have them briefly flash colors.) The following programs implement these ideas:

```

TO BLOCKS
  THIS PROCEDURE CLEANS UP THE
  SCREEN AND GETS BUILD STARTED
  TELL TELL
  SETCOLOR 0 CARRY 0
  HOME
  CLEARSCREEN
  TELL 0
  BUILD
  END

  BUILD
  THIS PROCEDURE TAKES A
  SINGLE KEY STROKE AS INPUT
  AND MAKES IT TO CHANGE
  SPRITE SHAPE, COLOR,
  NUMBER AND LOCATION
  CALL BC ANSWER
  IF ANSWER = "M" WEST
  IF ANSWER = "R" BACKONE
  IF ANSWER = "C" SETCOLOR COLOR
  IF ANSWER = "S" SETHEAD 0
  IF ANSWER = "N" SETHEAD 0 0
  FORWARD 00 : MOVE THE SPRITE
  TEN STEPS UP
  IF ANSWER = "D" RETRAILING 000
  FORWARD 10 : MOVE THE SPRITE
  TEN STEPS DOWN
  IF ANSWER = "S" RETRAILING 100
  FORWARD 00 : MOVE THE SPRITE
  TEN STEPS LEFT
  IF ANSWER = "D" RETRAILING 00
  FORWARD 10 : MOVE THE SPRITE
  TEN STEPS RIGHT
  IF ANSWER = "R" FORWARD
  IF ANSWER = "C" STOP : STOPS
  THE PROGRAM
  BUILD
  END
  
```

```

TO REAR
  THIS PROCEDURE REVERTS
  THE REAR SPRITE
  TEST TOCNUMBER = 01
  LEFT PRANT REAR AND NO MORE
  SPRITE LEFT : STOP
  IF CALL YOURNUMBER = 0 :
  END CARRY 0 STOP
  END

  TO BACKONE
  THIS PROCEDURE MOVES BACK
  TO THE "PROSELY"
  ALLOCATED SPRITE
  TEST YOURNUMBER = 0
  LEFT PRANT THIS IS THE FIRST 0
  SPRITE STOP
  IF TELL YOURNUMBER = 0 : 0 :
  ASK STOP
  END

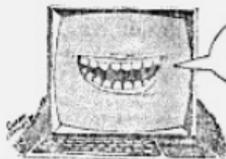
  TO FORWARD
  THIS PROCEDURE MOVES
  FORWARD TO BE CHANGED
  TEST SHAPE = 11 : IT IS THE
  LAST BLOCK AND A THE
  0 : IN THE BLOCK SET
  MOVE 10 FAR : CHANGING
  THIS NUMBER WOULD MAKE
  A LARGER SET
  IF CARRY 0 : START OFF WITH
  THE FIRST BLOCK IN THE
  SET
  IF CARRY 1 SHAPE = 1
  CHANGE THE SHAPE TO THE
  SHAPE IN THE SET
  END
  
```

```

TO FLASH
  THIS PROCEDURE TURNS
  OFF THE SPRITE OR FLASHES
  WHAT THE SPRITE WILL FLASH
  PROMPTLY TO IDENTIFY THE
  CURRENT SPRITE
  CALL COLOR "TART
  IF START = 0 FLASHES STOP
  FLASH : START STOP : GAMES
  THE SPRITE TO FLASH AND
  FINISH FLASHING WITH THE
  ORIGINAL COLOR ONLY WHEN
  THE COLOR ISN'T COLOR 0
  IF ANSWER 0
  END

  TO FLASH START
  SETPAT 5 : SETCOLOR 0 WAIT 20 0
  SETCOLOR : START WAIT 20 0
  END

  TO FLASHES
  SETPAT 5 : SETCOLOR 1 WAIT 20 0
  SETCOLOR 0 WAIT 20 0
  END
  
```



## The LOGO Poet: USING RECURSION FOR LIST HANDLING

Since TI LOGO's graphics capabilities are so vast and so easy to use, there is a tendency to overlook its other features. List handling is a case in point: By combining some of LOGO's list primitives—such operations as FIRST, BUTFIRST, (or the converse LAST, BUTLAST)—with recursive [see adjoining *A Primer on Recursion and List Primitives*] OUTPUT lines, we can easily write programs to reverse a list, alphabetize a list, or even compose poetry. The several examples that follow will, I hope, demonstrate to you the powerful simplicity and list-manipulation potential of the language.

Verifying the presence or absence of a word in a list is a problem commonly encountered in list processing. The MIT LOGO group refers to this as the "MEMBER?" problem because the program is to answer the question, "Is a specified word in a specified list?" Some aspects of the program are obvious. For example, once the answer is obtained (whether TRUE or FALSE), it should OUTPUT to the user or program which called for the answer. It is also obvious that if the list is empty, the word is not in the list. Given just this much information, it is possible to frame a MEMBER? program:

```
TO MEMBER? WORD LIST
  IF LIST = [] OUTPUT FALSE
  IF FIRST LIST = WORD OUTPUT
  TRUE
  OUTPUT MEMBER? BUTFIRST LIST
END
```

apert, following Polya, notes that one way of solving a complex problem is to ignore the complex whole and focus on those parts which can easily be solved. [See *Mindstorms: Children, Computers, and Powerful Ideas* by Seymour Papert—available from the 99'er Bookstore.] In the "MEMBER?" problem, if the first word in the list were the target word, then it would be easy to detect it and solve the problem using the LOGO primitive FIRST\*, which returns the first word in a list:

```
TO MEMBER? WORD LIST
  IF LIST = [] OUTPUT FALSE
  IF FIRST LIST = WORD OUTPUT
  TRUE
  OUTPUT MEMBER? BUTFIRST LIST
END
```

Now all that remains is solving for those cases in which the word is in an interior position or is absent from the list.

Were the word second in the list, the problem would be solved by adding a line using the LOGO primitive BUTFIRST, which returns all but the first word in a list of words:

```
IF FIRST BUTFIRST :LIST = :WORD OUTPUT
  TRUE
```

since the second word in the list is the first word in a list which excludes the first word. Similarly, the third word becomes the FIRST of the BUTFIRST\* of the BUTFIRST of the list, the fourth word is the FIRST of the BUTFIRST of the BUTFIRST of the BUTFIRST of the list. It would be possible to write a separate line for each of those positions as well as the fifth, sixth, seventh or any other potential word position. However, a program that did this would quickly grow ponderous. Fortunately, in LOGO this is unnecessary. Notice that for each position an additional BUT FIRST is all that is needed. The problem therefore requires only a single recursion line to complete the program:

```
TO MEMBER? WORD LIST
  IF LIST = [] OUTPUT FALSE
  IF FIRST LIST = WORD OUTPUT
  TRUE
  OUTPUT MEMBER? BUTFIRST LIST
END
```

Now when we run the program by typing MEMBER? [A QUICK BROWN FOX] "FOX, the first stack checks to see if the list is empty or if the first word in the list matches the target word, FOX. Then it awaits the results of a second stack which runs MEMBER? with the truncated list and the target word. The second stack then awaits the results of a third stack which runs MEMBER? on BROWN FOX and "FOX. That stack then awaits the results of MEMBER? FOX "FOX which returns "TRUE (from the match in the second line). "TRUE is returned to the second stack which outputs "TRUE to the first stack which outputs "TRUE to the program which first called it (or to top level). In the event that there were no matches, one of the stacks would eventually run MEMBER? on an empty list and would output "FALSE.

Another common problem is to count the number of words in a list of words. As before, this problem is solved by outlining the obvious elements of the solution and the simplest case.

```
TO COUNT :LIST
  OUTPUT some number
END
```

The simplest case occurs when the list is empty.

```
TO COUNT :LIST
  IF :LIST = [] OUTPUT 0
  OUTPUT some number
END
```

When a list has just one word in it, the program should recognize that and OUTPUT 1. Since a list with just one word is one word away from an empty list, The LOGO

\* FIRST returns the first word in a list of words, or the first letter in a list of words, or the first letter in a word. LAST returns the last letter in a list of words, or the last letter in a word. BUTFIRST returns all but the first word in a list of words, or all but the first letter in a word. BUTLAST returns all but the last word in a list of words, or all but the last letter in a word.

operation **BUTFIRST** applied to that list would yield the empty list. If there were two words in a list, then obviously the list is just two words away from an empty list. If a recursive line were added into the program which (a) applied **BUTFIRST** and (b) added 1 to the count for every application of **BUTFIRST**, the program would count the words in the list.

```

TO COUNT LIST
  IF LIST = [] OUTPUT 0
  ELSE COUNT BUTFIRST LIST
END

```

For another example, consider a program which will reverse a list. The simplest case would be a list with no words.

```

TO REVERSE [] OUTPUT
END

```

The next simplest case would be a list with just one word. For such a list we could have the program **OUTPUT** the **SENTENCE** of the word and an empty list.

```

TO REVERSE [SENTENCE] OUTPUT SENTENCE []
  IF LIST = [SENTENCE] OUTPUT SENTENCE []
  ELSE REVERSE BUTLAST LIST
END

```

This solution can be applied to longer lists as well.

For a final example, let's use **LOGO** to "write" random poetry. As a first effort at **LOGO** poetry, we'll attempt some "free verse" by instructing a poet to string words together randomly from a list we select. First, we will need a program like **SELECT** to output a selected item from a list.

```

TO SELECT LIST
  IF N = 0 OUTPUT FIRST LIST
  OUTPUT SELECT (N - 1) BUTFIRST LIST
END

```

Then we need a program to generate random numbers for **SELECT**. Because **LOGO**'s **RANDOM** primitive provides the integers through nine, if our list is less than ten, we can get a **COUNT** of it as that **COUNT**.

```

TO NUMB LENGTH
  CALL RANDOM N
  TEST BOTH N > 0 & N < LENGTH
  IF N = 0
  IF N OUTPUT N
  IF N OUTPUT NUMB LENGTH
END

```

By first typing

```
CALL COUNT LIST "LENGTH
```

we can then use **NUMB** for the value of **LENGTH**. If we then type:

```
TYPE SELECT (NUMB LENGTH) [a list of words]
```

the computer types one of the words in the list. We can write that as a program:

```

TO Verse LIST
  TYPE SELECT (NUMB LENGTH) LIST
  NUMB
END

```

## A PRIMER ON RECURSION AND LIST PRIMITIVES

It is easier to understand recursion in **LOGO** if one imagines that each **LOGO** program is a job for a contractor to perform. Each contractor is a specialist and can do only one job. Every contractor follows strict working rules; these rules say that when the contractor sees **STOP**, he must stop, when he sees **OUTPUT**, he must pass back some information and then stop. Of course, when a contractor reaches an **END**, he also stops. When a contractor sees the name of any **LOGO** program in use, the program he is completing, he subcontracts that job to another contractor. Thus, in **COUNT** (A, B, C), the first contractor reads the first line of the program, but the condition can't met, so he moves to line two. There he is told to **OUTPUT 1 + the COUNT of [B, C]**. Since he can't do another program, he subcontracts the job. The subcontractor reads line 1 of **COUNT** and since it doesn't apply, he reads line 2. He is told to **OUTPUT 1 + the COUNT of [C]**. He can't do that, so he also subcontracts that job. The third contractor sees that line 1 doesn't apply and line 2 tells him to **OUTPUT 1 + the COUNT of []**. He is so lucky that he can't subcontract the job out, and so the fourth contractor reads line 1 of **COUNT**. Since the list is empty, he **OUTPUTS 0** and passes the job back to the third contractor; he in turn adds 1 and then **OUTPUTS 2**. The first contractor adds 1 to that and then **OUTPUTS 3**, which is the correct answer. With this explanation, you should now be able to analyze a program which gives you the answer to a number **X** raised to the **N** power.

```
TO EXPONENT X N
```

```

  .
  .
  .
  END
  TO EXPONENT X N
  IF N = 0 OUTPUT 1
  .
  .
  .

```

```
END
```

```
TO EXPONENT X N
```

```

  IF N = 0 OUTPUT 1
  IF N = 1 OUTPUT X
  OUTPUT (EXPONENT X N - 1) * X
  END

```

To turn this into a line of poetry, we should have a random number of such randomly picked words with a random number of spaces between words (E. E. Cummings's style) and then a carriage return:

```

TO SPACE
  TREAT RANDOM (PRINTCHAR 32)
  END
  TO LINE LIST
  REPEAT RANDOM (SPACE VESE LIST)
  PRINT SELECT (NUMB LENGTH) LIST
  END

```

Note: **PRINTCHAR 32** puts the character with ASCII code 32, a space, on the screen.

If we want continuing lines of poetry, we can write a recursive program:

```

TO LINE LIST
  LINE PRINT
  LINE LIST
  END

```

Now, putting this all together we get:

```

TO POEM LIST
  CALL COUNT LIST LENGTH
  LINE LIST
  END

```

Now we can try converting POET into a program which produces either rhyming verse, blank verse, or a finite number of lines of verse. One way to modify POET to produce rhymed verse is to give it two different lists—one of words for the interior words of each line of verse, and another of rhyming words for the last word in each line. Then the program can be changed so that only rhyming words are placed in end positions.

```

TO LINES LIST RHYMES
LINES MUST ACCOMMODATE TWO
LINES
LINE LIST RHYMES
LINES LIST RHYMES
END

TO POET LIST RHYMES
THE SECOND LIST MUST NOW BE
GIVEN THE PROGRAM
CALL COUNT LIST LENGTH
CALL COUNT RHYMES LENGTH
NECESSARY TO FIND OUT HOW
MANY RHYMING WORDS THERE
ARE
LINES LIST RHYMES
END

TO LINE LIST RHYMES
LINE MUST PUT RHYMES ONLY AT
THE END OF EACH LINE
REPEAT RANDOM SPACE VERSE 11
PRINT SELECT I NUMS LENGTHS
RHYMES
PUTS A RHYME AT THE END
END

TO SPACE
RE 32
END

TO COUNT LIST
IF LIST = 1 OUTPUT 0
OUTPUT I COUNT RHYMES LIST
I N
END

TO NUMS LENGTHS
CALL RANDOM M
TEXT SIZE M * 8 * N * 1 LENGTH
M * N
IF OUTPUT M
IF OUTPUT NUMS LENGTHS
END

TO SELECT N LIST
IF N = 1 OUTPUT FIRST LIST
OUTPUT SELECT N - 1 BUTFIRST
LIST
END

TO VERSE LIST
TYPE SELECT I NUMS LENGTHS
LIST
END

```

You probably recognize that the problem of generating rhyming verse is one form of the problem of teaching the computer to write text which follows a specified rule (in this case each line must rhyme). The more general application of rules to text is nothing less than grammar. One of the grade school pupils in the Brookline project wrote a text-book rule program like POET which generated random sentences. After she saw the effects of changing parts of speech she exclaimed enthusiastically that she now understood what a noun was.

POET can also be quickly adapted to a sentence generator which young people can play with to make grammar meaningful.

```

TO SENTENCES
PRINT "HERE A LIST OF ARTICLES
AND THEN PRESS ENTER
CALL READLINE "ART
PRINT "TYPE A LIST OF NOUNS AN
D THEN PRESS ENTER
CALL READLINE "NOMS
PRINT "TYPE A LIST OF ADJECTI
VE S AND PRESS ENTER
CALL READLINE "ADI
PRINT "TYPE A LIST OF VERBS AN
D THEN PRESS ENTER. NOW WATCH.
CALL READLINE "VERBS
GRAMMAR ART NOMS ADI VERB
S
END

TO GRAMMAR ART NOMS ADI V
ERBS
TYPE SELECT I NUMS I COUNT AD
I "ART
SPACE
TYPE SELECT I NUMS I COUNT NO
UNS I I "NOMS
SPACE
TYPE SELECT I NUMS I COUNT VE
RBS I "VERBS
SPACE
TYPE SELECT I NUMS I COUNT AD
I "ADI
SPACE "ADI
TYPE SELECT I NUMS I COUNT NO
UNS I I "NOMS
PRINT
WAIT 30
GRAMMAR ART NOMS ADI VERB
S
END

```

SENTENCES can be made a better grammarian by adding distinctions of number and gender where appropriate; it can be made a more sophisticated language generator if GRAMMAR is altered to allow for conjunctions and subordinate clauses. All of these changes and more can be programmed by students as they learn both the specifics of grammar<sup>1</sup> and the mathematics of LOGO.

<sup>1</sup> Paper would probably argue that most students know the grammar which schools attempt to teach, but that the students do not have verbal labels for syntactical rules and parts of speech, and do not see the relevance of the labels once they are told them. A sentence generator program can make grammar "speech syntactic."

# Avoiding Turtle Traps



Seymour Papert and his colleagues purposefully decided to structure LOGO to facilitate the writing of good computer programs. The concept of good programming is not superficially apparent. Of course, a program should accomplish its intended goal, but all programmers recognize that any goal can be achieved by many different types of programs. Beyond simply "working," there are a number of criteria by which programs can be judged. Programs which have multiple applications are generally better than single-purpose programs. Programs which are easier to debug and which can be understood by people other than the authors (or which can be understood by the authors at a future time) are more desirable. Pragmatically, programs which run faster or with fewer bits of memory are better than slower or more memory-intensive programs. Finally, some programs are aesthetically more appealing than others.

It is possible to find examples of program applications in which two or more of the criteria are in conflict. However, it is more often the case that the criteria are in accord. All of the criteria except for aesthetics are straightforward and relatively objective. Still, writing aesthetic programs is so satisfying that aesthetics will be considered first here.

For instance, you can write GO in LOGO, but programs with many different branches from GO commands are particularly inelegant. Why write poor programs when good ones are easier to write? Also inelegant are programs with hundreds of lines of code, especially when the code contains several repetitions of a series of commands. And programs with many inputs are generally less aesthetic than those with fewer inputs. Compare the aesthetics of two programs which count the number of words in a list:

```

TO COUNT
  IF SUBFIRST LIST = 1 OUTPUT
  COUNT ON 1 SUBFIRST LIST
END
    
```

This program requires typing as input along with COUNT and the list in question requires a starting value of :N-0.

```

TO COUNT
  IF LIST OUTPUT 0
  OUTPUT 1 COUNT SUBFIRST LIST
END
    
```

This program requires no superfluous input.

Elsewhere in this chapter, there is a fairly complex program, DYNATURTLE, which creates a turtle that obeys Newtonian laws of motion. Despite the complexity of the program, DYNATURTLE is relatively elegant: DYNATURTLE has only three lines, which are INITIALIZE, SETDYNATURTLE, and CONTROL. Each of those lines is, in turn, a brief program which serves a unique function. Contrast DYNATURTLE's elegance with a spaghetti-pole BASIC program which would achieve the same effects. Such a program would be long and littered with extensive GO-TO's.

A subtler example of elegant and inelegant programs can be made from the GRAMMAR program. The program was modified from an earlier POET program and was written:

```

TO GRAMMAR
  ART NOUNS ADJ VERB
  TYPE SELECT ( NOUNS ) COUNT :N
  SPACE
  TYPE SELECT ( NOUNS ) COUNT :NO
  USE 0 0 CHECKS
  SPACE
  TYPE SELECT ( NOUNS ) COUNT :VE
  USE 0 0 CHECKS
  SPACE
  TYPE SELECT ( NOUNS ) COUNT :AD
  USE 0 0 CHECKS
  SPACE
  TYPE SELECT ( NOUNS ) COUNT :VO
  USE 0 0 CHECKS
  PRINT
  WAIT 50
  GRAMMAR ART NOUNS ADJ VERB
  END
    
```



sion call and before END. The garbage collector sees that there is a line of commands and cannot tell that the line is useless, so it is barred from refurbishing the memory! Empty lines use up memory and can block garbage collection (depending on their location), so empty lines should be eliminated from your programs.

Finally, the operating system can work faster when fewer sprites are being used, i.e., programs which use no sprites run faster than programs which use sprites. The more sprites in use (generally), the slower the system operates. The reason for the slight degradation in response time is obvious—the system has to check to see which, if any, sprites must be displayed or moved. The system checks on its sprites by looking up the highest number of sprite called upon. For example, TELL 31 or TELL SPRITE 31 would cause the system to check on every sprite from 31 on through to sprite 0. Such a check is necessary (from the user's perspective) only if all 32 sprites are being used. If only one sprite is needed, then the user should type TELL 0 or TELL SPRITE 0 and the system would skip the checkup on sprites 1 to 31, thus saving a small amount of time.

#### Student Reactions to a Four Week LOGO Class By Gene Branum

Students pick up these principles quickly. For instance, Gene Branum, a student in a four-week LOGO course, reflects on this experience:

"The expectations of the students varied—we wanted to know more about computers, we wanted a different Jan-term experience, or maybe just a free Jan-term. Whatever the motivation, all came away affected in some way by our experience. All experienced both the frustration of failure and the flush of triumph as the computer finally 'did what it was supposed to.'

"The format for our experience was a four-week mini-term (Jan-term) at Austin College. Our class met; five days a week for two hours, and we were required to spend at least one hour of work on our own as well. This requirement was easily met; as one student put it, 'It was not unusual to spend four hours at a time' on the computer. Needless to say, the experience was very intense, and there was a great deal of self-teaching. This was felt to be one of the greatest strengths of the course.

"Professor Hank Gorman did a fine job of teaching the basics early in the course. As he told us his expectations, we scoffed. After two weeks, he told us, we would be drawing cartoons and making up games. Even though his leadership was great, the majority were insecure about 'the machine.' Our confidence, however, grew with experience and familiarization.

"The two greatest aspects of the course for all of us were (1) the team experience and (2) experience in general problem solving skills. The true strength of LOGO is that students, working together, can teach each other massive amounts of material. The realization that everyone had problems put us all on the same level. Sharing ideas and solutions became important for everyone because no one could work totally independently. Many social experiences allow students to interact, but LOGO is one of the few that forces students to *think together*.

"Without exception, all of the students involved in the course commented that, after LOGO, they knew better how to approach a complex problem. Dr. Gorman spent several class periods on problem solving skills: decomposition, recursion, naming, multiple descriptions, and the 'little men.' These skills not only aided our search for solutions to LOGO problems, but also for problems that require a thinking solution. The overriding principle of LOGO is that the simple builds to the complex, which is its major strength as a system for any age-group.

"While it was widely agreed upon that none of us 'mastered' LOGO, each of us developed confidence in our abilities to control the computer and make it do what we requested. The LOGO experience allowed everyone to use logical approaches to problem solving and gain valuable hands-on experience in a discipline that continues to increase in importance."

The following programs, which students wrote during this course, show an emerging appreciation for elegance, speed, and simplicity in programming. Except for correction of typographical errors, their work hasn't been edited in an attempt to find still more elegant ways of achieving their programs' goals. Note, however, that they all grasp the essentials of esthetic programming.

### Space Pylon Racer

Once set up, the player guides his saucer through pylons. Two shapes must be made first (check graph paper). The keys control the saucer. E moves it upward, X moves it downward, D moves it forward, S moves it backward, F speeds it up, A slows it down. If the ship hits a pylon, the beep sounds.

Use arrow keys to change direction.  
Use F for fast speed.  
Use A for slow speed.

```

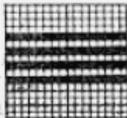
TO GAME
CO:
TELL "ALL SS SC CARRY
SETI
TELL
SPK
END
  
```

```

TO CHECK
TEST BOTH : BOTH ECOR - 85 TC
CO: - 15 : BOTH TCOR - 74
TCOR - 80
LFT GO
TEST BOTH : BOTH ECOR - 85 TC
CO: - 15 : BOTH TCOR - 54
TCOR - 70
LFT GO
TEST BOTH : BOTH ECOR - 85 TC
CO: - 115 : BOTH TCOR - 74 TC
R - 80
LFT GO
TEST BOTH : BOTH ECOR - 85 TC
CO: - 115 : BOTH TCOR - 54 TC
R - 70
LFT GO
TEST BOTH : BOTH ECOR - 15 TC
CO: - 85 : BOTH TCOR - 70 TC
ON - 85
R - 85
TEST BOTH : BOTH ECOR - 15 TC
CO: - 85 : BOTH TCOR - 50 TC
ON - 85
LFT GO
END
  
```



MAKESHAPE 20  
Saucer



MAKESHAPE 21  
Pylon

```

TO GET
TELL 0 CARRY 20 SC RED 500
1000 0
TELL 1 1 2 3 4 5 6
CARRY 20 SC BLACK
TELL 1 500 - 50 00
TELL 2 500 - 50 00
TELL 3 500 - 50 00
TELL 4 500 - 50 00
TELL 5 500 100 00
TELL 6 500 100 00
END

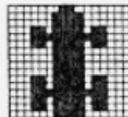
TO SPR
CONTROL
CHECK
SPR
END

TO CONTROL
IF RCY = TRUE THEN TEST 3 = 4
TELL STOP
CALL SC
IF 2 = 1 - 2 TELL 0 50 0 STOP
IF 2 = 1 - 2 TELL 0 50 100 STOP
IF 2 = 1 - 2 TELL 0 50 200 STOP
IF 2 = 1 - 2 TELL 0 50 300 STOP
IF 2 = 1 - 2 TELL 0 50 400 STOP
IF 2 = 1 - 2 TELL 0 50 500 STOP
END

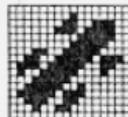
```

### Spinout

This program was designed as a cartoon to depict two Indianapolis-style racing cars racing, crashing, burning, and being towed away. The central program, SPINOUT, contains 7 subprograms. These short programs make the central program neat and concise.



MAKESHAPE 6



MAKESHAPE 7

```

TO SPINOUT
WAIT
MOVE
WAIT 500
SMERVE
WAIT 20
SPIN
WAIT 50
BURN
TOW
END

TO SETOP
TELL 0
CARRY 6
SC 0 50 0 50 0
HOME
TELL 1 CARRY 6
SC 0
50 0 50 0
HOME
TELL 0 50 15
END

```

```

TO MOVE
TELL 5 CARRY 0
SC 1
TELL 4 CARRY 10
SC 1
TELL 3 50 - 70 50 0
TELL 2 50 50 0
SC 10
BITOP
TELL 4 10FEAT 4 15 5 WAIT 10
SC 10 WAIT 10 SC 15 WAIT 10 SC
10 1
WAIT 50
HOME
END

```

```

TO MOVE
TELL 0
SC 10
TELL 1 50 10
TELL 2 4 1 SC 0
END

```

```

TO SMERVE
TELL 0
REPEAT 10 10 - 5 WAIT 5 50 0
WAIT 5 50 - 2 WAIT 5 50 10 WAIT
5 10
SC 15
END

```

```

TO SPR
CALL 10 1 1 TEAM
TELL TEAM SC 10
REPEAT 5 CARRY 6 WAIT 5 CARRY
8 WAIT 5 CARRY 6 WAIT 5 CARRY
7 WAIT 5 CARRY 6 WAIT 5 CARRY
6 WAIT 5
END

```

```

TO BURN
REPEAT 10 10 6 WAIT 5 50 11 W
AIT 5 50 0 WAIT 5
TELL TEAM
SC 1 50 0
SC 7
END

```

```

TO TOW
TELL 5 CARRY 10
SC 0
SC 100
SC 1 - 70
WAIT 100
SC 200
SC 30
WAIT 115
SC 0 WAIT 200
CALL 10 1 5 1 7
TELL 0
SC 50
SC 10
WAIT 75 SC 0 50 0
END

```

```

TO MUNCHIE
SETOP
MOVE
END

```

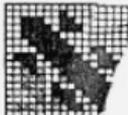
### Munchie

Munchie illustrates how one can program a sprite to move to certain locations where an object may be found. After testing coordinates within the procedure, it eats that object and continues on until it eats all objects. You move Munchie by using arrow keys, and set speed by using keys 0, 5, and 1. You should stop Munchie when passing over the object to be eaten.

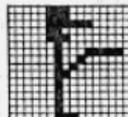
```

TO MUNCHIE
SETOP
MOVE
END

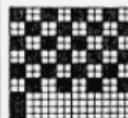
```



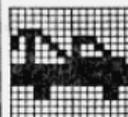
MAKESHAPE 8



MAKESHAPE 9

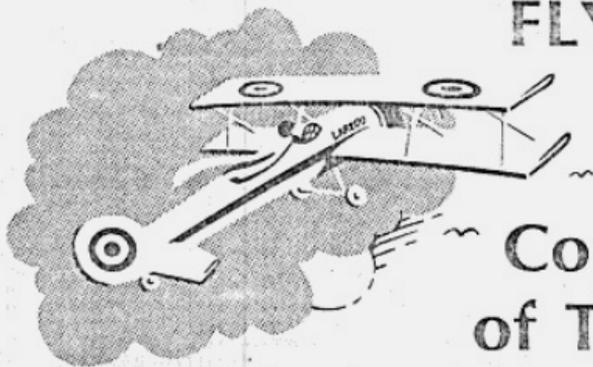


MAKESHAPE 10



MAKESHAPE 11





# FLY AWAY

with the

# JOY

# Commands of TI LOGO

You push the stick forward, and the aircraft begins to roll. You then gradually pick up speed and start moving down the runway. After reaching takeoff speed, you move the stick again, and suddenly you're airborne. Now you have control of the skies—to fly high or low, do loops and other maneuvers, and then land. But be careful with your speed! You don't want to stall and crash.

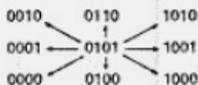
This isn't flight training or a simulator. It is a TI LOGO procedure that gives you the opportunity to fly by keyboard or joystick. It uses either the arrow keys or the JOY 1 and JOY 2 commands. The JOY commands return one of nine values depending on the position of the joystick, thus opening a wide range of possibilities for interactive games and other activities.

At first, it might appear that the nine values have little relationship to each other. You'll note that the three and the seven were omitted. However, the pattern of the values is quite interesting.



Moving from left to right in each row, you'll note that each digit is four more than the previous digit, i.e.,  $2 + 4 = 6$ ,  $6 + 4 = 10$ , etc. Moving from bottom to top in each column, observe that each digit is one more than the previous one.

These patterns begin to suggest why three and seven were omitted from the values assigned. However, to make the logic behind these patterns even more graphic, let's convert them to binary numbers.



Now look at the first two digits in each column. You'll note that they are the same, representing from left to right, 0, 1, and 2. Also, if you look at the last two digits in each row, you'll note that they are also the same. Moving from bottom to top, they also represent 0, 1, and 2. So what we really have here is a distinctive coordinate system with real meaning, rather than what might first be perceived as a random placement of values.



Let X and Y be used to name these coordinates. The coordinates for the joysticks can be assigned with the command.

```
MAKE "Y (JOY1) / 4
MAKE "X (JOY1) - 4 * :Y
```

Now let's put these JOY commands to work in FLYAWAY, a procedure developed by Roger Kirchner, a fellow YPLA member. This is a procedure for one or two players that tests each player's ability to take off and safely land an airplane on the runway shown on the screen. Either the direction keys on the keyboard or the joysticks can control the plane.

The joystick commands are incorporated in the procedure, STICK S. Push the stick forward, and the aircraft increases its speed.

```
IF :X = 6 THEN FASTER
```

Pull the stick back and the aircraft slows down:

```
IF :X = 4 THEN SLOWER
```

To minimize the chance for error, direction commands are accessed by merely moving the joystick to the left or

right. It does not matter whether you hit position 0, 1, 2; the aircraft will turn left.

```
IF :X > 4 THEN TURNLEFT
IF :X < 6 THEN TURNRIGHT
```

Of course, it would be possible to add additional maneuvers using each of the nine joystick positions. This would require a much more sensitive touch to the joystick, but that could also add to the challenge of the flight.

With each turn of the aircraft, a new shape is called to show that new position. These range from #10 through #18. The first shape, #10, is similar to the Plane shape in TI LOGO. The next shape shows the aircraft at a 45° angle. The other shapes depict the plane in a 90° angle, 135° angle, at 180°, 225°, 270° and 315°. Shape #18 depicts the crash.

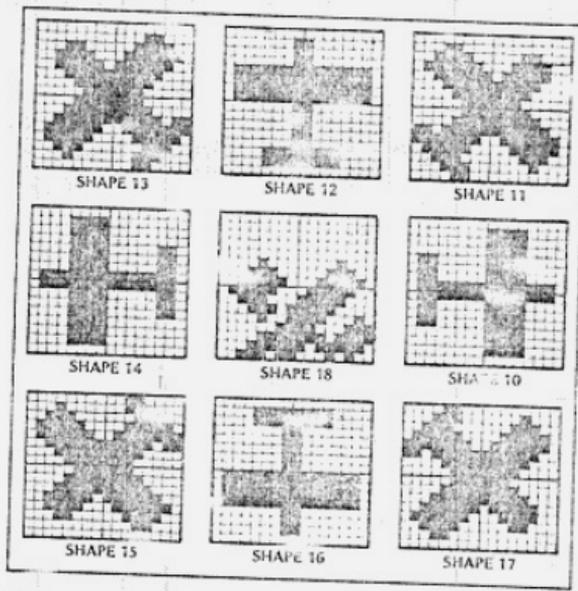
The CONTROLJOY and the CHECK P procedures control the aircraft in the air. CHECK P monitors the speed and "altitude" of the aircraft to test for the CRASH parameters.

FLYAWAY is an excellent graphics program that begins to tap the power of the LOGO language. It goes quite a bit further than merely drawing pictures with the computer. This is an important point to realize. But unfortunately, not all educators do. In a November issue of *InfoWorld*, one educator stated that although he can understand young peo-

ple enjoying maybe 50 to 100 hours of drawing pictures with LOGO, he would imagine they would then tire of language and move on to the other things.

Do chess players ever tire of chess? Do chess masters ever feel that they have mastered the game? Probably not. The moves of chess can be easily learned by primary grade youngsters, but entire *lifetimes* are spent learning the game. Certainly the graphics capabilities and the speed of LOGO are spectacular. Indeed, they tend to overshadow the other attributes of the language. Where that happens it is most unfortunate because LOGO offers a young person so much more than just graphics—much more than BASIC and some other high level languages.

For example, look closely at BASIC: It uses a fine number of commands that must be strung together in statements that tend to hide the operation of the program. Were the operation of BASIC programs easily discernible, TRACE would be unnecessary. LOGO, on the other hand is a virtually unlimited language. If the command does exist, use your imagination and create it! This is the marvellous challenge of TI LOGO—using your imagination and creativity to discover the *real* potential of the computer. Way back in the dark ages before microcomputer Albert Einstein expressed a truth that is especially relevant to today's computer learning environments: "Imagination is more powerful than knowledge." Undoubtedly, Einstein would have approved of TI LOGO.



```
TO SETUP
CS
VANISH
PRINT "INSTRUCTIONS: Y = 1
IF RC = Y THEN HELP MAKE X 1
CS
PRINT "NAME OF BLUE PILOT?
MAKE "BLUE PILOT "REDDING
PRINT "NAME OF RED PILOT?
MAKE "RED PILOT "REDDING
PRINT "FLIGHT WITH KEY CONTROL
S OF JOYSTICK: 1 = 2
MAKE "MODE "REDDING
MAKE "YSS "40
MAKE "YSP "50
MAKE "UDOWN "50
MAKE "DOWN "72
CS
END

TO FLYAWAY
SETUP
FORWARD
LEFT CONTROL
LEFT CONTROLJOY
END

TO CONTROL
MAKE "X "0
IF "X = "0 THEN TELL "FASTER
IF "X = "1 THEN TELL "FASTER
IF "X = "2 THEN TELL "FASTER
IF "X = "3 THEN TELL "FASTER
IF "X = "4 THEN TELL "FASTER
IF "X = "5 THEN TELL "FASTER
IF "X = "6 THEN TELL "FASTER
IF "X = "7 THEN TELL "FASTER
IF "X = "8 THEN TELL "FASTER
IF "X = "9 THEN TELL "FASTER
IF "X = "0 THEN TELL "FASTER
IF "X = "1 THEN TELL "FASTER
IF "X = "2 THEN TELL "FASTER
IF "X = "3 THEN TELL "FASTER
IF "X = "4 THEN TELL "FASTER
IF "X = "5 THEN TELL "FASTER
IF "X = "6 THEN TELL "FASTER
IF "X = "7 THEN TELL "FASTER
IF "X = "8 THEN TELL "FASTER
IF "X = "9 THEN TELL "FASTER
CHECK 1 CHECK 2
CONTROL
END
```

```

TO KLF
CS
PRINT "FLYWAY"
PRINT
PRINT ELSE PILOT USES KEYS E
  S D X OR JOYSTICK
PRINT
PRINT KID PILOT USES KEYS J
  I E M OR JOYSTICK
PRINT
PRINT CONTROLS
PRINT
PRINT FASTER E J OR STICK TO
WARD
PRINT SLOWER X M OR STICK BA
CK
PRINT TURN LEFT S J OR STICK
LEFT
PRINT TURN RIGHT D E OR STIC
K RIGHT
PRINT
PRINT
PRINT USE WHO CAN TAKE OFF AN
D LAND SAFELY FIRST
PRINT
PRINT SOM VOYAGE
END

TO VANISH
TELL ALL HOME SS 0 SS 0 CARRY
0
END

TO CONTROLGY
STICK 1 CHECK 1
STICK 2 CHECK 2
IF RCY THEN STOP
CONTROLGY
END

TO SETPLANE P
IF P = 1 THEN MAKE YS YS E
LSE MAKE YS YS
TELL Y SC 0 2 H P - 2 I SY
YS YS 0 34 38 CARRY 10
END

```

```

TO STICK S
MAKE Z JOY 3
TELL Z
IF Z = 4 THEN TURNLEFT
IF Z = 5 THEN TURNRIGHT
IF Z = 6 THEN FASTER
IF Z = 4 THEN SLOWER
END

TO CRICK P
TELL P
IF SPEED = 10 THEN STOP
IF FCOR = 10 THEN STOP
TELL COUNTER FCOR X UPOFF FCOR
X DOWNOFF
OFF CRASH
OFF IF SPEED = 8 THEN WELCOME
ELSE STOP
WAIT 120
CC PLANE WHO
END

TO TURNRIGHT
RT 45
IF SHAPE = 10 THEN CARRY 17 EL
SE CARRY SHAPE - 1
END

TO TURNLEFT
LT 45
IF SHAPE = 10 THEN CARRY 10 EL
SE CARRY SHAPE - 1
END

TO SLOWER
IF SPEED > 0 THEN SS SPEED - 5
END

TO FASTER
IF SPEED < 100 THEN SS SPEED +
5
END

```

```

TO FLUSH N
IF N = 1 THEN OUTPUT N = 1
ELSE OUTPUT 10
END

TO MIXES M
IF M = 0 THEN OUTPUT N = 1
LSE OUTPUT 57
END

TO WELCOME
PRINT "PRICE LANDING"
I PILO
T WHO
END

TO CRASH
PRINT "SO GOOD"
PILOT
WHO
MAKE "DROP FCOR - 1 - 50"
A
IF " - 50" = " DROP + 10"
IF " > 0" THEN MAKE " " " - 1
CARRY 10
SS 0
END

TO PILOT N
IF N = 1 THEN OUTPUT PILOT
ELSE OUTPUT PILOT
END

TO RUNWAY
TELL TILL 00 50 (2 YS)
TELL TILL 100 50 GREEN
MAKE TILES 100 100 100 0
0 100 100 100 100
MAKE FROM 15
A
IF TILES = 1 THEN STOP
MAKE "COOL"
EPCAT 52 197
IF COOL FROM MAKE
IF COOL COOL
MAKE TILES RT TILES
MAKE FROM FROM + 1
GO A
END

```

# Problem Solving WITH LOGO

It is pleasurable to work with a language like LOGO because it gives us something to "think with," and it encourages us to think in what Papert has called "mind-sized bites." The solution of a problem can be identified with the definition of a procedure. If the problem is simple, we can specify the procedure directly. Otherwise, we try to specify it in terms of a small number of simpler procedures.

Often, this method leads to a complete solution of a problem. But sometimes, a problem is so complex that the method leads to an indefinite number of problems. A solution seems hopeless.

But suppose that new problems have the same form as previously encountered problems, and are simpler. The problem will be solved at least "theoretically," if the rules lead to a solution in a finite number of steps. Such a solution is said to be recursive.

One of the beauties of a language such as LOGO is that recursive procedure definitions are allowed. And writing a LOGO procedure not only gives a theoretical solution, but a practical one which can be carried out by executing the procedure. Of course, for the latter, one needs access to a TI-99/4A with TI LOGO (or some other implementation of LOGO).

In thinking through the solution of a problem, one often works "both ends." The big picture leads to smaller pictures, but also details occur which can be incorporated into procedures, which then make the solution of larger problems easier.

## Translating the Pig Latin

As a concrete example of these ideas, consider the momentous task of translating an English word into Pig Latin. According to my children, the rule is to add "HAY" at the end of a word beginning with a vowel, otherwise to take the consonant sound from the front, add "AY" to it, and put it at the end. Thus "AND" translates to "ANDHAY", and "BREAK" translates to "EAKBRAY."

These rules lead immediately to a LOGO procedure for accomplishing the task:

```

TO HELP
  CS PRINT [FOR FIGLATIN PRACTICE]
  E
  PRINT TYPE "FIGLATIN"
  END

TO FIGLATIN
  CS
  PRINTING [I WILL HELP]
  PRINTING [YOU LEARN FIGLATIN]
  A
  PRINT
  PRINTING [TYPE A SENTENCE]
  MAKE [LONG STRAINE]
  IF LONG = 0 THEN PRINTING [
  THAT WAS FUN STOP]
  PRINTING [LINE]
  CS [A]
  END
  
```

```

TO TRANWORD [W]
  IF [K H S THEN MAKE "VOWELS [A
  E I O U]]
  IF [K H S THEN MAKE "VOWELS [A
  E I O U]]
  TEST MEMBER FIRST W VOWELS
  IF [0] THEN WORD W AY
  IF [OUTPUT TRANWORD] [WORD
  FIRST W FIRST W]
  END

TO TRANWORD W
  TEST MEMBER FIRST W [A E I O
  U]
  IF [OUTPUT TRANWORD W]
  IF [OUTPUT TRANWORD] W
  END
  
```

```

TO PRINTING [LINE]
  TEST [LONG W]
  IF [PRINTING] [S
  IF [TYPE TRANWORD] [LINE]
  IF [PRINTING] [LINE]
  END

TO TRANWORD W
  OUTPUT WORD W HAY
  END

TO MEMBER [S]
  IF [SET W] THEN OUTPUT [AL
  SE
  TEST [S - FIRST SET]
  IF [OUTPUT TRUE]
  IF [OUTPUT MEMBER] S BY [SET]
  END
  
```

```

TO TRANWORD W
  TEST MEMBER FIRST W [A E I O
  U]
  IF [OUTPUT TRANWORD W]
  IF [OUTPUT TRANWORD] W
  END
  
```

This procedure reduces our problem to the solution of three simpler problems, which we might need to reduce further. The procedures we need are:

```

MEMBER object list
TRANWORD word
TRANWORD word
  
```

MEMBER returns TRUE if *object* is in *list* and returns FALSE otherwise. TRANWORD translates *word* if it begins with a vowel. TRANWORD translates *word* if it begins with a consonant. We can hope that MEMBER is a utility built into LOGO. It isn't, but this is no problem. Nearly anything that isn't a primitive can be built in.

At any stage in the solution process we can decide to work on big problems or focus on little ones. The solution of a problem isn't a linear process, even if solutions are usually presented as if the process were orderly and straightforward. The LOGO procedures document and organize progress.

Let's focus on the problem of deciding membership. If *object* is in a list, it is either the first item of the list, or else



it is the first of a truncated list, or it is not in the list. The definition is, naturally, recursive:

```
TO MEMBER X SET
  IF SET = 1 THEN OUTPUT 'FAL
  SET
  TEST X = FIRST SET
  IF OUTPUT TRUE
  IF OUTPUT MEMBER X BY SET
  END
```

With this definition, MEMBER FIRST :W [A E I O U] will return TRUE if :W begins with a vowel, and FALSE if it doesn't.

The definition of TRANVWORD is so simple we can write the procedure anytime. Let's do it now:

```
TO TRANVWORD W
  OUTPUT WORD W 'HAY
  END
```

The (undocumented) primitive WORD takes two words as input and outputs the word formed by joining them.

The definition of TRANWORD takes more thinking. We want it to be recursive. We want to move letters from

the beginning to the end until the first letter is a vowel, and then add "AY". We are led to:

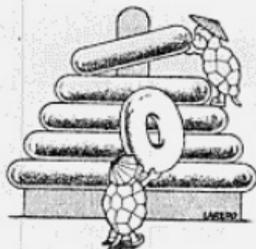
```
TO TRANWORD W
  TEST MEMBER FIRST W [A E I O U]
  IF OUTPUT WORD W 'AY
  IF OUTPUT TRANWORD | WORD BY
  TEST FIRST W FIRST W
  END
```

If we try (that is, think through, or execute in LOGO) TRANWORD "BREAK, we find it will return EAKBRAY, as desired. And TRANWORD "YOU returns OUYAY. But TRANWORD "BY runs out of space because the recursion cannot end. Evidently Y must be added to the list of vowels. But then TRANWORD "YOU would return YOUHAY and not OUYAY.

Can you fix this bug? We want Y to count as a vowel only if it isn't the first letter. One solution is to use two inputs to TRANWORD, one of which is a flag. This solution, as well as the generalization to translating a sentence, can be seen by reading the PIGLATIN procedure and the procedures it calls.

PIG

## TOWER OF HANOI



```
TO NUMMOVES N
  TEST N = 1
  IF OUTPUT 1
  IF OUTPUT 1 - 2 * N NUMMOVES
  N - 1
  END
```

Trying this procedure, we find that NUMMOVES 2 = 3, and also that NUMMOVES 3 = 7. The reader might try to find a formula for NUMMOVES *n*, and also the value of NUMMOVES 64.

Of more interest is a procedure for actually solving the puzzles, and beyond that, for implementing the solution graphically. By the above reasoning, what we need is a procedure SOLVE with four inputs:

SOLVE *n* *peg1* *peg2* *peg3*

which would move the top *n* rings from *peg1* to *peg2* using *peg3*. Using the rules we obtain:

```
TO SOLVE N P1 P2 P3
  TEST N = 1
  IF GETRING P1 SETRING P2
  IF SOLVE N - 1 P1 P3 P2
  SOLVE N P1 P2 P3
  SOLVE N P2 P1 P3
  END
```

To have LOGO print out the moves in order, we need to implement two procedures called GETRING and SETRING:

In the meantime, let's implement GETRING and SETRING simply so we can test our solution:

```
TO GETRING P
  TYPE 'PICK GO | PRINTCAR 32
  TYPE P PRINTCAR 32
  END
```

Now we turn to a less frivolous example. The Tower of Hanoi is a puzzle familiar to many. It consists of three pegstands. One contains a "tower" of circular rings. The object is to move the tower from one peg to another, moving one ring at a time, and never putting a larger ring on top of a smaller one. There is rumored to be a Buddhist priest working on a puzzle with 64 rings; when he finishes, the world will end. If he makes one move per second, how much should we worry?

We can use LOGO to worry about this problem. We need a procedure, say NUMMOVES, which takes for input the number of rings and outputs the number of moves. Suppose we think of the task this way: Move the top *n* - 1 rings to an auxiliary peg, then move the largest ring, then move the smaller *n* - 1 rings onto the largest.

The way of viewing the problem leads to the following recursive definition for NUMMOVES:

```

TO SOLVE3 [P]
  TYPE [SET ON 1] PRINTMAN 32
  PRINT [P]
  END

```

Now, if we enter SOLVE 2 "A "B "C, the output will be:

```

PICK UP A SET ON C
PICK UP A SET ON B
PICK UP C SET ON B

```

The number of moves for three rings is 3, as expected. What will be the seven moves for SOLVE 3 "A "B "C? Try it!

We've looked at a LOGO procedure for solving the Tower of Hanoi as an abstraction. This procedure, SOLVE, prints out—as a list—the sequence of moves necessary for the solution. But given the graphics power of LOGO, we should be able to design a program—a series of procedures—which will represent the actual movement of rings from one peg to another graphically. And, in fact we can use LOGO's MAKECHAR command to define the required graphics, called tiles, and we can move these newly-defined tiles about, using LOGO procedures. So let's begin at the beginning.

Let A, B, and C be the three pegs. When we know which rings are on which pegs, we then know the particular state of the puzzle. In our LOGO implementation, the variables A, B, and C will be the names for lists which tell us which rings are on each peg. Our puzzle will have 8 rings. Let us name them 1 through 8 in order of increasing size. The beginning position, with all rings on peg A, is represented by :A = [1 2 3 4 5 6 7 8], :B = [], and :C = []. Moving the top ring from A onto B results in the state :A = [2 3 4 5 6 7 8], :B = [1], :C = []. In essence, a move consists of removing a number from the beginning of one list and adding it to the beginning of another list. At the same time, of course, the graphic representation ring must be erased and redisplayed in the correct position.

Let us first construct a procedure HANOI, which will allow us to play with the puzzle and then, when we want, solve it automatically.

```

TO HANOI
  INITIALIZE
  SETUP
  PLAY
  SETUP
  SOLVE B "A "B "C
  END

```

INITIALIZE should set colors and define constants. SETUP should display the puzzle with all the rings on peg A. PLAY should allow us to pick rings up and put them down by simply pressing the names of the corresponding pegs. Play might continue until 'Q' is pressed. The puzzle should then be redisplayed and solved automatically, beginning with the rings on peg B. The procedure SOLVE was developed in the previous section. Procedures SETUP, PLAY, and SOLVE will depend on workhorse procedures GETRING and SETRING. The requirements for INITIALIZE will become apparent as we make choices about representation.

Assume that INITIALIZE assigns the value 8 to N and :TOP is the number of the ring to be displayed. Then SETUP can be:

```

TO SETUP
  CS [ ]
  STAMP 'A
  STAMP 'B
  STAMP 'C
  MAKE 'TOP N
  MAKE 'A [ ]
  MAKE 'B [ ]
  MAKE 'C [ ]
  REPEAT N [ SETRING 'A MAKE 'TO
  P 'TOP - 1
  END

```

Using utilities MEMBER?, EMPTY, and ALARM, we can write PLAY in such a way as to validate all inputs. We want to accept either 'Q' or to stop PLAY the letters A, B, and C only. (VALID will be initialized to [A B C].) We also want to prevent an attempt to remove a ring from an empty peg. If an error is made, we will cause an alarm to be sounded. (See the listing for definitions of the utilities.)

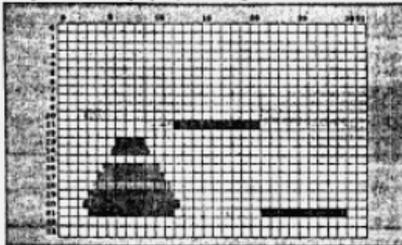
```

TO PLAY
  [ ]
  MAKE 'X AC
  IF B = [ ] TO TALK STOP
  IF NOT MEMBER? X VALID THEN
  ALARM GO 'H
  IF EMPTY THING X THEN ALARM
  GO 'L
  GETRING X
  [ ]
  MAKE 'X AC
  IF NOT MEMBER? X VALID THEN
  ALARM GO 'L
  SETRING X
  PLAY
  END

```

In this procedure, note that the value of X, :X, is the name of a peg, either A, B, or C. One might expect that the value of :X would be denoted :X, but this denotes the value of 'X'. The primitive THING must be used. THING :X is the list named by :X.

In order to discuss GETRING and SETRING, we need to be specific about how to represent the graphics. We could use the turtle, but we choose tiles because this allows the most colorful display. The LOGO screen is divided into 32 columns numbered 0 to 31 from left to right, and 24 rows numbered 0 to 23 from top to bottom. We can place the rings on the display by locating them relative to their





Before anything will happen, though, the tiles must be defined using MAKECHAR. (See figures.) Then, ENJOY! Recall that to manipulate the rings, you just need to press the letter of the peg from which you want to take, or to which you want to add a ring. Use the procedure HELP if you forget.

After you have had some fun with the puzzle, you might want to try a four peg variation. To implement a four peg version, do the following:

Change INITIALIZE to include:

```
MAKE "VALID [ A B C D ]
MAKE "ABASE [ 8 10 ]
MAKE "BBASE [ 24 10 ]
MAKE "CBASE [ 8 23 ]
MAKE "DBASE [ 24 23 ]
```

In SETUP, add:

```
MAKE "D [ ]
STAND "D
```

The puzzle should then contain four pegs: A, B, C, and D. It can be manipulated just like the three peg puzzle. The

automatic solution will still use just three pegs. But as a worthy challenge, you might try to write a better version of SOLVE which takes advantage of the fact that there are two auxiliary pegs instead of just one. The puzzle should take fewer moves to solve. How many less than  $2n - 1$  moves are required if there are  $n$  rings and four pegs? I would be interested in any of your results. Then can five pegs be fit on the screen. . . ?

But if you are looking for a lesser challenge, or just want to experiment with a simpler puzzle, note that the number of rings is set in INITIALIZE and can be changed. Try this: Enter INITIALIZE, and then MAKE "N 5 (or some other integer). If you now enter SETUP, a puzzle with 5 rings will be displayed. Enter PLAY, and you can manipulate this puzzle until you press Q. Now enter SETUP again, and then SOLVE 4 "A "C "B. This will cause four rings to be moved automatically to peg C. Then enter PLAY and you can complete the puzzle by yourself. With LOGO, the procedures are your own to do with or modify as you please. Use your imagination, make up other puzzles, or just go ahead and play with this section's puzzle as is.

```
TO BANDI
  INITIALIZE
  SETUP
  PLAT
  SETPT
  SOLVE B "A "B "C
END

TO INITIALIZE
  TELL TELL 86 SC "BLACK
  TELL TELL 984 SC "WHITE
  TELL TELL 412 SC "RED
  TELL TELL 178 SC "ORANGE
  TELL TELL 628 SC "YELLOW
  TELL TELL 136 SC "LIME
  TELL TELL 844 SC "OLIVE
  TELL TELL 952 SC "SKY
  TELL TELL 648 SC "SLUE
  TELL TELL 648 SC "PUFFLE
  MAKE "N 8
  MAKE "VALID [ A B C ]
  MAKE "ABASE [ 8 10 ]
  MAKE "BBASE [ 24 10 ]
  MAKE "CBASE [ 8 23 ]
  MAKE "DBASE [ 24 23 ]
END

TO PLAY
  LN
  MAKE "X SC
  IF "N = 0 THEN STOP
  IF NOT MEMBER? X VALID THEN
    ALARM GO "X
  IF EMPTY? TRING X THEN ALARM
  GO "X
  GETRING X
  LIST
  MAKE "X SC
  IF NOT MEMBER? X VALID THEN
    ALARM GO "X
  SETRING X
  PLAT
  END

TO SETUP
  CS
  STAND "A
  STAND "B
  STAND "C
  MAKE "TOP "N
  MAKE "A [ ]
  MAKE "B [ ]
  MAKE "C [ ]
  REPEAT "N SETRING "A MAKE "TO
  END
```

```
TO ALARM
  BEEP
  WAIT 30
  BEEP
  BEEP
  END

TO MEMBER? X LIST
  IF LIST = 0 THEN OUTPUT "FA
  USE
  IF "N = FIRST LIST THEN OUTPUT
  SET "TRIC "X
  OUTPUT MEMBER? X IF LIST
  END

TO HELP
  CS
  PRINT TYPE "BANDI" TO BEGIN
  MAKE "X ROW 1
  PRINT "PUSH A, B, OR C TO RING
  VE OR SET DOWN A RING.
  PRINT "
  PRINT "ITG OUT, AND WATCH THE
  PRICLE SOLVED AUTOMATICALLY. P
  "USE D.
  END

TO STAND "P
  MAKE "SCORD TRING WORD "P "FA
  SE
  MAKE "COL FIRST "SCORD
  MAKE "ROW LAST "SCORD
  MAKE "X COL - "N "2
  REPEAT "X "2 "X "2 "1 PT
  SE "X ROW MAKE "X "1 "1
  MAKE "X ROW 1
  REPEAT "N (PT 184 "COL "E MAKE
  "X "1 "1 "X
  PT CHARNUM "P COL ROW + 1
  END

TO SETRING "P
  MAKE "P SC TOP TRING "P
  MAKE "SCORD TRING WORD "P "FA
  SE
  MAKE "COL FIRST "SCORD
  MAKE "X COUNT TRING "P
  MAKE "ROW LAST "SCORD "X
  SE
  DISPLAYING
  END
```

```
TO SOLVE "N "P1 "P2 "P3
  IF "N = 0 THEN GETRING "P1 SET
  SOLVE "N - 1 "P1 "P3 "P2
  GETRING "P1 SETRING "P2
  SOLVE "N - 1 "P3 "P2 "P1
  END

TO DISPLAYING
  MAKE "LT 184 + TOP + B
  MAKE "MID 185 + TOP + B
  MAKE "RT 186 + TOP + B
  PT MID COL ROW
  MAKE "X "1
  REPEAT TOP "2 (PT MID COL
  "X "1 "1
  ON MAKE "X "1 "1
  W "PT "COL + TOP "2 + 1 "FO
  W "PT "COL + TOP "2 + 1 "FO
  W
  END

TO CRASERING
  MAKE "X "N TOP "2
  REPEAT "X TOP "2 (PT 33 "CO
  "X "1 "1 "1
  ON MAKE "X "1 "1
  PT 184 "COL ROW
  END

TO COUNT LIST
  IF LIST = 0 THEN OUTPUT "X
  COUNT OF LIST
  END

TO GETRING "P
  MAKE "SCORD TRING WORD "P "FA
  SE
  MAKE "TOP FIRST TRING "P
  MAKE "COL FIRST "SCORD
  MAKE "X COUNT TRING "P
  MAKE "ROW LAST "SCORD "X
  SE
  CRASERING
  MAKE "P IF TRING "P
  END

TO EMPTY? LIST
  IF LIST = 0 THEN TRIC DETECT "D
  DC ELSE OUTPUT "FALSE
  END
```